

Computational Geometry Algorithms Library

Pierre Alliez INRIA

Mission Statement

"Make the large body of geometric algorithms developed in the field of computational geometry available for industrial applications"

CGAL Project Proposal, 1996

Algorithms and Datastructures



Bounding Volumes



Triangulations





Subdivision Simplification





Lower Envelope

Arrangement



Polyhedral Surface



Boolean Operations



Voronoi Diagrams



Parameterization Streamlines



Intersection Minkowski Detection Sum



Ridge Detection



PCA



Polytope

distance









CGAL in Numbers

500,000 lines of C++ code

- 10,000 downloads/year (+ Linux distributions)
 - 3,500 manual pages
 - 3,000 subscribers to cgal-announce
 - 1,000 subscribers to cgal-discuss
 - 120 packages
 - 90 commercial users
 - 20 active developers
 - 12 months release cycle
 - 2 licenses: Open Source and commercial

Some Commercial Users



CGAL Open Source Project

Project = « Planned Undertaking »

- Institutional members make a long term commitment: Inria, MPI, Tel-Aviv U, Utrecht U, Groningen U, ETHZ, GeometryFactory, FU Berlin, Forth, U Athens
- Editorial Board
 - Steers and animates the project
 - Reviews submissions
- Development Infrastructure
 - Gforge: svn, tracker, nightly testsuite,...
 - 120p developer manual and mailing list
 - Two 1-week developer meetings per year

Contributions

- Submission of specifications of new contributions
- Review and decision by the Editorial Board
- Value for contributor
 - -Integration in the CGAL community
 - -Gain visibility in a mature project
 - Publication value for accepted contributions

Exact Geometric Computing

Predicates and Constructions



Robustness Issues

- Naive use of floating-point arithmetic causes geometric algorithms to:
 - Produce [slightly] wrong output
 - Crash after invariant violation
 - Infinite loop
- There is a gap between
 - Geometry in theory
 - Geometry with floating-point arithmetic

Geometry in Theory

ccw(s,q,r) & ccw(p,s,r) & ccw(p,q,s) ® ccw(p,q,r)



Correctness proofs of algorithms rely on such theorems

Demo: The Trouble with Double orientation(p,q,r) = sign($(p_x-r_x)(q_y-r_y)-(p_y-r_y)(q_x-r_x)$) q (24, 24) negative zero positive x = yr (0.5 + ϵ_x , 0.5 + ϵ_y) р (0.5, 0.5)

Exact Geometric Computing [Yap]

Make sure that the control flow in the implementation corresponds to the control flow with exact real arithmetic





Filtered Predicates

- Generic functor adaptor Filtered_predicate<>
 - -Try the predicate instantiated with intervals
 - In case of uncertainty, evaluate the predicate with multiple precision arithmetic
- Refinements:
 - Static error analysis
 - Progressively increase precision

Filtered Constructions

Lazy number = interval and arithmetic expression tree Lazy object = approximated object and geometric operation tree



Test that may trigger an exact re-evaluation:

if (n' < m')

if (collinear(a',m',b'))

The User Perspective

- Convenience Kernels
 - Exact_predicates_inexact_constructions_kernel
 - Exact_predicates_exact_constructions_kernel
 - Exact_predicates_exact_constructions_kernel_with_sqrt
- Number Types
 - double, float
 - CGAL::Gmpq (rational), Core (algebraic)
 - CGAL::Lazy_exact_nt<ExactNT>
- Kernels
 - CGAL::Cartesian<NT>
 - CGAL::Filtered_kernel<Kernel>
 - CGAL::Lazy_kernel<NT>



Merits and Limitations

- Ultimate robustness inside the black box
- The time penalty is reasonable, e.g. 10% for 3D Delauny triangulation of 1M random points
- Limitations of Exact Geometric Computing
 - Topology preserving rounding is non-trivial
 - Construction depth must be reasonable
 - Cannot handle trigonometric functions

Generic Programming

STL Genericity

```
template <class Key, class Less>
class set {
  Less less;
  insert(Key k)
  {
     if (less(k, treenode.key))
       insertLeft(k);
     else
       insertRight(k);
}:
```

CGAL Genericity

```
template < class Geometry >
class Delaunay_triangulation_2 {
   Geometry::Orientation orientation;
   Geometry::In_circle in_circle;
```

void insert(Geometry::Point t) {

```
if(in_circle(p,q,r,t)) {...}
...
if(orientation(p,q,r){...}
}
```

p

CGAL Genericity Demo

Without explicit conversion to points in the plane

- Triangulate the terrain in an xy-plane
- Triangulate the faces of a Polyhedron



Summary: Overview

- Open Source project
- Clear focus on geometry
- Interfaces with de facto standards/leaders: STL, Boost, GMP, Qt, blas
- Robust and fast through exact geometric computing
- Easy to integrate through generic programming