

A generative model for the joint registration of multiple point sets

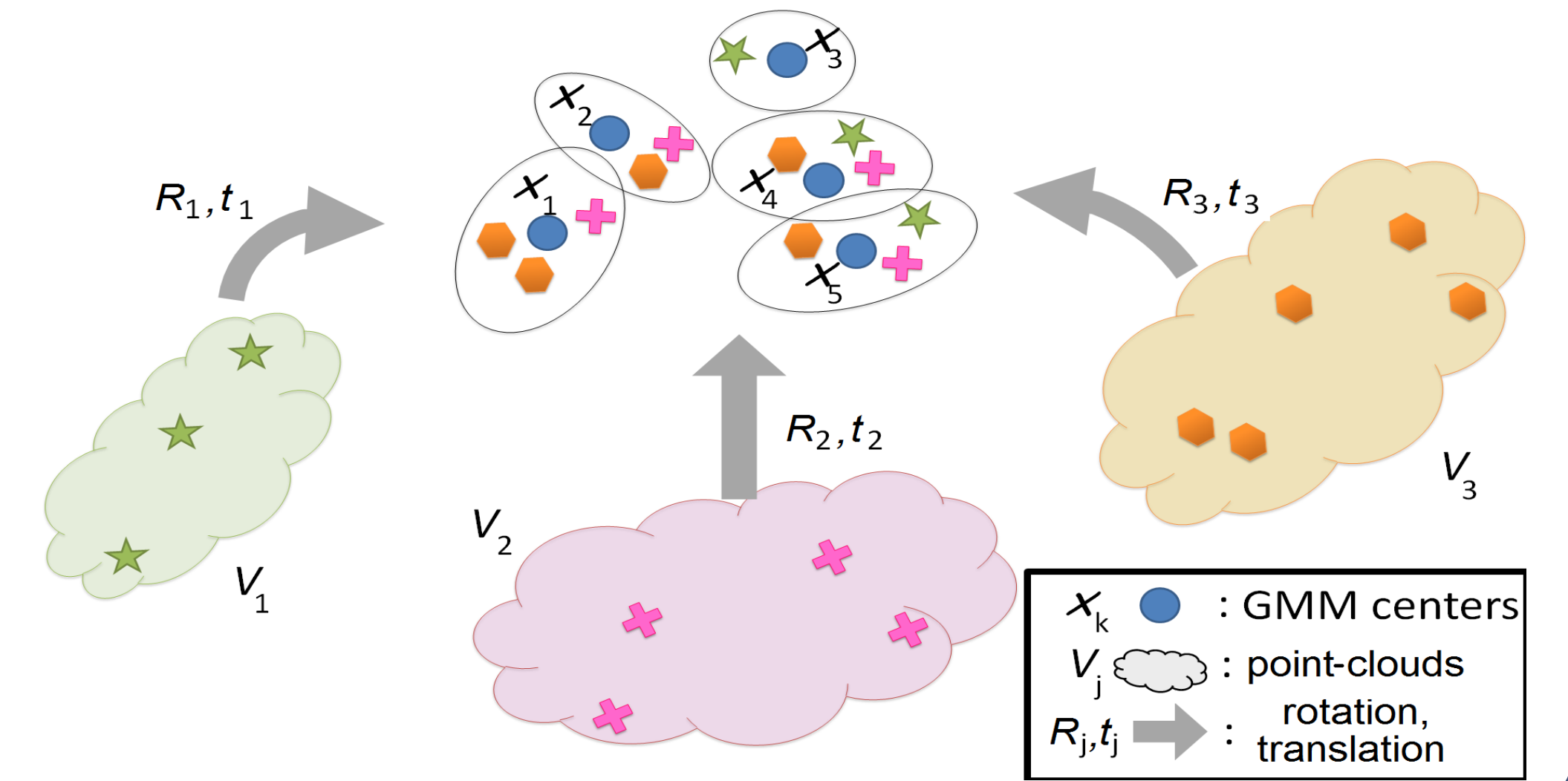


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I. Abstract

We propose a generative model and its associated algorithm for the joint registration of multiple point clouds. **All the point sets** are assumed to be **rigidly transformed realizations** of a Gaussian Mixture Model (GMM), whose means play the role of a central scene model. A formally derived Expectation Conditional Maximization (ECM) algorithm estimates both the GMM parameters and the rigid transformations (one per set), so that the point sets can be jointly registered without favoring any particular set.



2. The model

If v_{ji} denotes the i -th 3d point of the j -th point set, its realization is modeled by a mixture of K Gaussian and one uniform components

$$P(v_{ji}) = \sum_{k=1}^K p_k \mathcal{N}(\phi_j(v_{ji}); \mathbf{x}_k, \Sigma_k) + p_{K+1} \mathcal{U}(h)$$

with $\phi_j(v_{ji}) = R_j v_{ji} + t_j$ where

R_j, t_j : 3D rotation/translation of j -th set,

\mathbf{x}_k, Σ_k : means/variances of the Gaussian components

p_k : prior terms of the mixture

h : the volume that encompasses all the data

This leads to an augmented parameter set of mixture parameters and transformations that has to be estimated:

$$\Theta = \left\{ \{p_k, \mathbf{x}_k, \Sigma_k\}_{k=1}^K, p_{K+1}, \{R_j, t_j\}_{j=1}^M \right\}$$

3. The algorithm

We introduce a hidden variable z_{ji} , such that $z_{ji} = k$ assigns a transformed observation $\phi_j(v_{ji})$ to the k -th mixture component, and we aim to maximize the **expected complete-data log-likelihood**. This reduces into the constrained optimization problem:

$$\begin{aligned} \max_{\Theta} f(\Theta) \\ \text{s.t. } R_j^T R_j = I, |R_j| = 1, \forall j \end{aligned}$$

where

$$f(\Theta) = -\frac{1}{2} \sum_{jik} a_{jik} \left(\left\| \phi_j(v_{ji}) - \mathbf{x}_k \right\|_{\Sigma_k}^2 + \log |\Sigma_k| - 2 \log p_k \right) + \log p_{K+1} \sum_{ji} a_{ji(K+1)}$$

and $a_{jik} = P(z_{ji} = k | v_{ji}; \Theta)$ is the posterior probability of an assignment. An ECM scheme is adapted to this problem, thus yielding a novel algorithm that is called **JR-MPC (Joint Registration of Multiple Point Clouds)** and follows the outline:

Initialize Θ

Repeat until convergence

E-Step: estimate posteriors

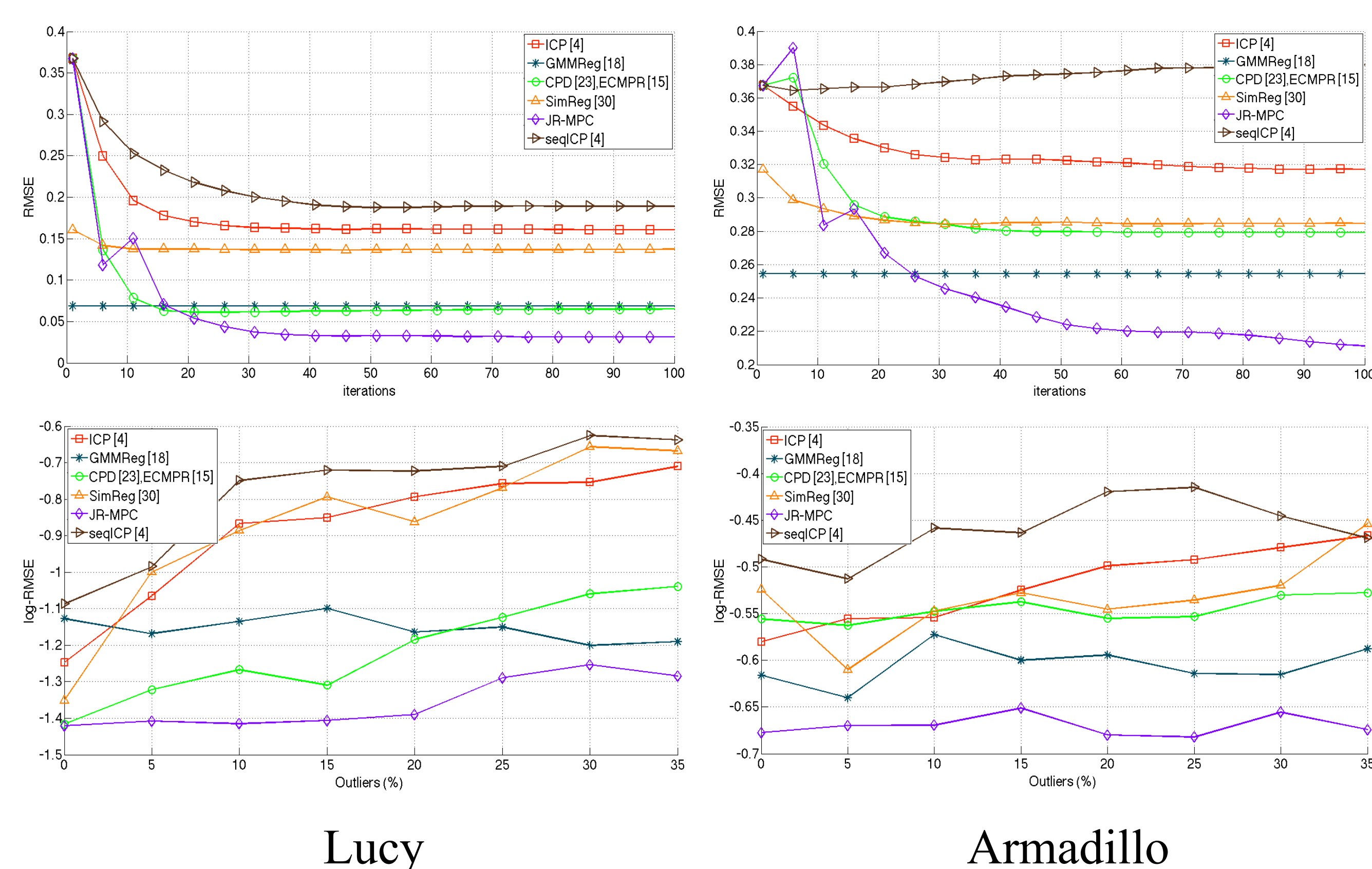
CM-Step-1: use current mixture parameters to update transformation

CM-Step-2: use current transformations to update mixture parameters

4.1 Results on synthetic data-sets

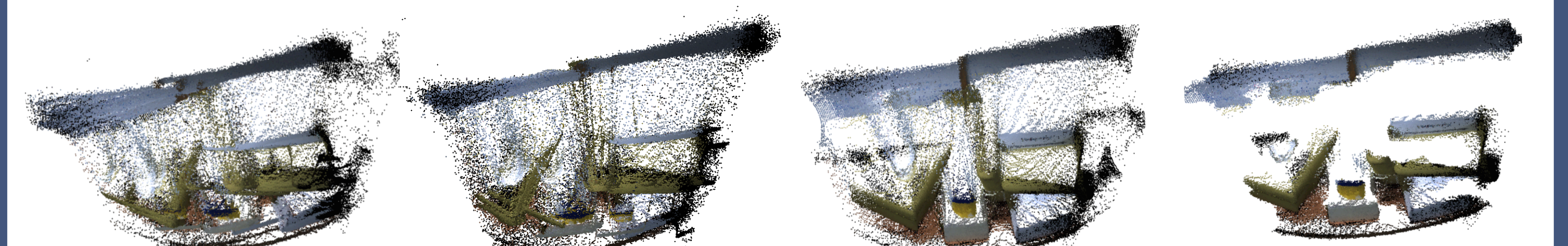
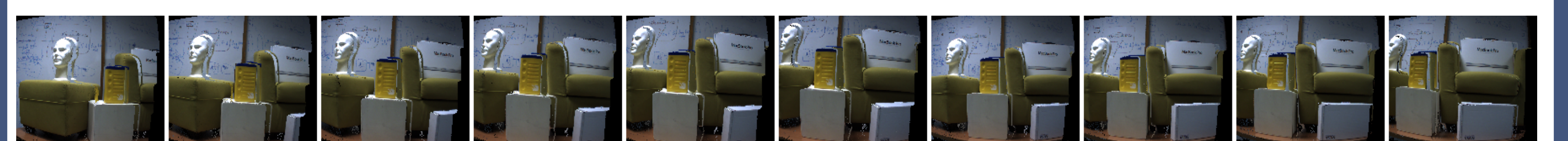
Registration of four **partially-viewed** point sets of a 3D model

- 10-degree rotation between successive views
- different down-sampling per point set
- point noise and outliers were added
- Root MSE of rotation error is used for evaluation



4.2 Results on real data-sets

Ten point clouds captured by moving a TOF camera around a scene (color is used for visualization)



Sequential ICP [4]

SimReg [30]

JR-MPC

JR-MPC after outlier rejection

See also our videos!

5. Conclusions

- A probabilistic model to jointly register multiple point sets is proposed.
- The proposed method treats all the point sets on an equal footing.
- An ECM-based algorithm estimates an augmented parameter set that consists of GMM parameters and rigid transformations.
- As a by-product, an outlier-free scene model is reconstructed (see our videos).

References

- [4] Besl & McKay: A method for registration of 3D shapes. PAMI (1992)
- [15] Horaud et al.: Rigid and articulated point registration with expectation conditional maximization. PAMI (2011)
- [23] Myronenko & Song: Point-set registration: Coherent point drift. PAMI (2010)
- [30] Williams & Bennamoun: Simultaneous registration of multiple corresponding point sets. CVIU (2001)
- [18] Jian & Vemuri: Robust point set registration using Gaussian mixture models. PAMI (2011)

