

Modeling and Control of heterogeneous Traffic in cities

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Inria
INVENTEURS DU MONDE NUMÉRIQUE

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Complex Cities



Sub

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CONTROL

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$$\int_{t_0}^{t_f} [n_1(t) + n_2(t)] dt + \sum_{k=0}^{K-1} \sum_{l=1}^L x_l(k)$$

$n_{1,2}(k)$



$n_{23}(t)$

$$\frac{dn_{12}(t)}{dt} = q_{12}(t) + q_{123}(t) + \hat{q}_{312}(t) - u_{12}(t) \cdot M_{12}(t)$$

$$\frac{dn_{13}(t)}{dt} = \frac{q_{213}(t)}{q_{213}(t) + q_{21}(t)} u_{21}(t) \cdot M_{21}(t) + q_{13}(t) - \min(M_{13}(t), C_{or,1}(t))$$

$$+ q_{213}(t) + \hat{a}_{321}(t) - u_{21}(t) \cdot M_{21}(t)$$

$$\frac{dn_{23}(t)}{dt} = \frac{q_{123}(t)}{\hat{q}_{312}(t) + q_{12}(t)} + q_{22}(t) + q_{132}(t) + q_{32}(t) + q_{23}(t) + q_{231}(t) - \min(M_{23}(t), C_{or,2}(t))$$

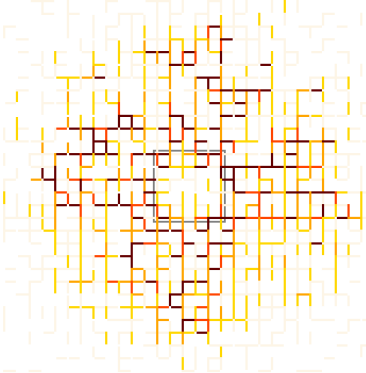
$$+ q_{23}(t) + q_{231}(t) - \min(M_{23}(t), C_{or,2}(t))$$

$$x = (n_{or,i}(k)) / I_k$$

$$u_{1,2}(t) \leq u_{max} ; u_{min} \leq u_{or,1}(k), u_{or,2}(k) \leq u_{max}$$

$$n_{1,2}(t) = n_{1,2}(t)$$

$$n_{1,2}(t) = n_{1,2}(t)$$



PATTERNS

LUTS team



Nikolas Geroliminis



Jack Haddad (PostDoc) (CE – Control)



Konstantinos Aboudolas (Post Doc) (EE)



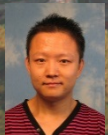
PhD Students



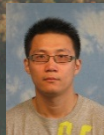
Burak Boyaci (OR)



Mohsen Ramezani (EE)



Yuxuan Ji (CS)



Nan Zheng (CE)



Mehmet Yildirimoglu (CE)

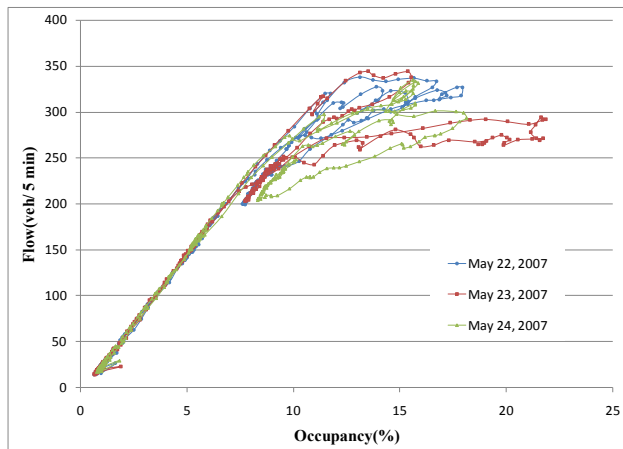


Big challenges in complex transport systems

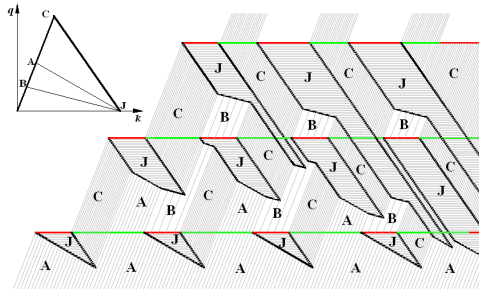
Non-linear interactions

- Components influence the system and vice versa
- Components adapt
- Causes and effects not proportional - Hysteresis
- Spreading phenomena
- Transient states

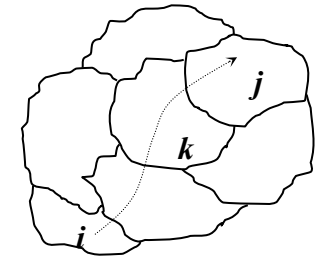
- Limits to predictability
- Complex Dynamics
- Chaotic Behavior
- Sensitivity



- Limits to Control
- Instabilities
- Irreducible randomness
- Local Optima
- Multi-objective Optimization
- State Estimation



$$\frac{dn_{ij}}{dt} = q_{ij} - \sum_{k=1}^N q_{i \rightarrow k}^j + \sum_{k=1}^N q_{k \rightarrow i}^j$$



MODELING

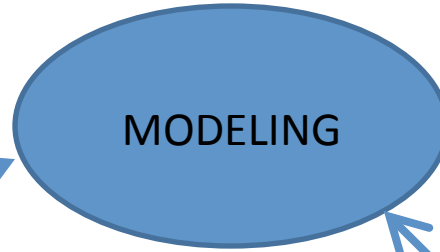
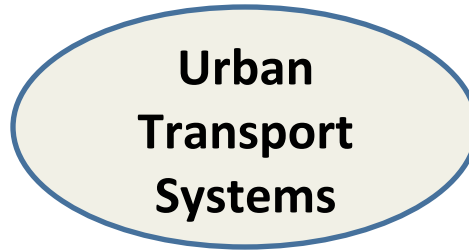
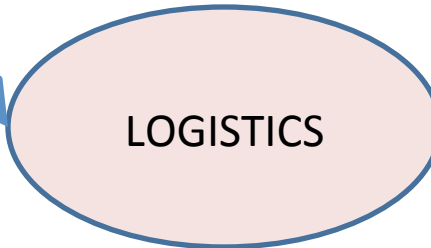


MANAGEMENT
& CONTROL

Urban
Transport
Systems

MONITORING

LOGISTICS

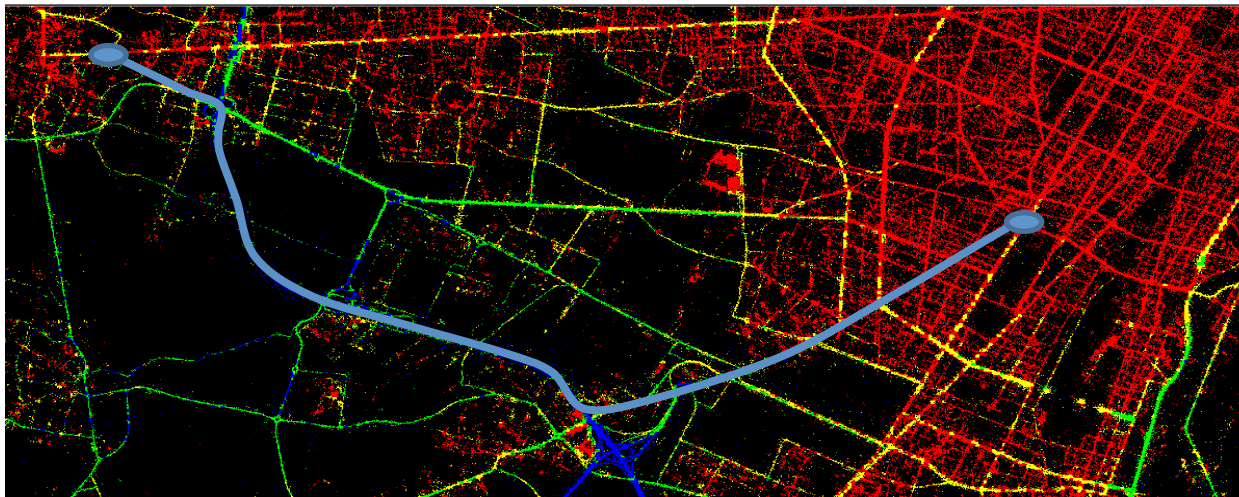
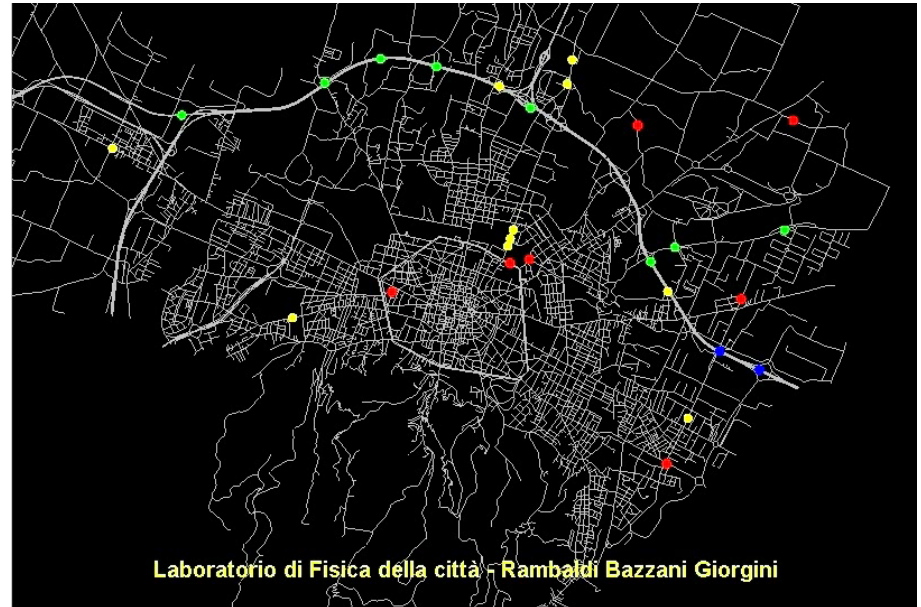


MONITORING

Heterogeneity

- Spatial and Temporal
- Congestion Level
- Topology
- Modes of transport
- Sensing equipment
- Spatiotemporal correlations

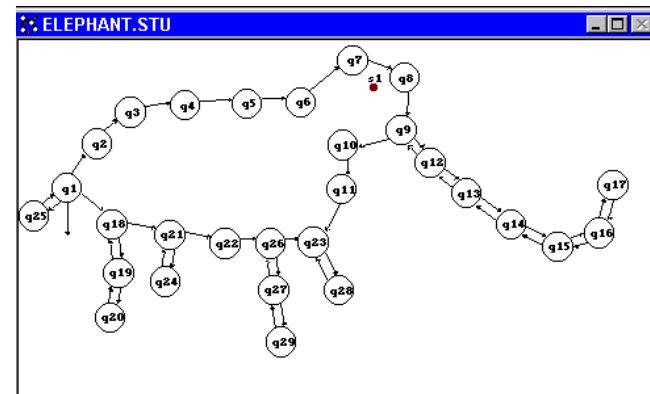
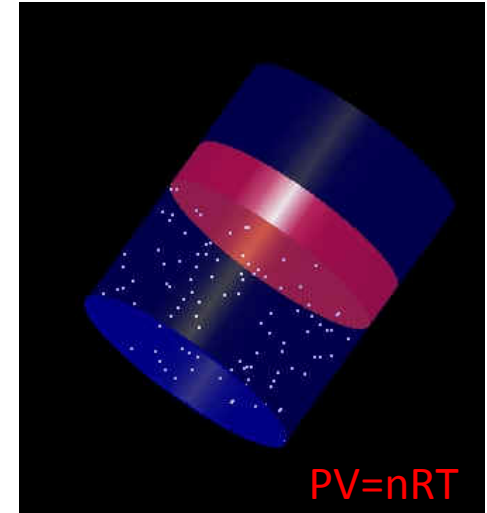
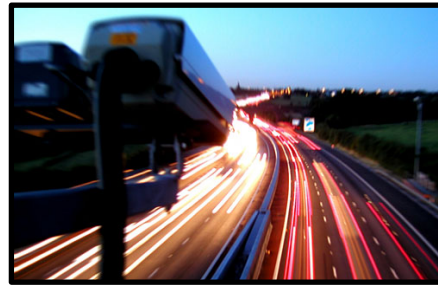
Sparse multi-sensor data



Pictures provided
by Prof. Bazzani

WHY AGGREGATED?

- Humans make choices in terms of routes, destinations and driving behavior (unpredictability – related to control)
- Not a clear distinction between free-flow and congested traffic states (complexity of traffic states)
- Need for real-time hierarchical traffic management schemes



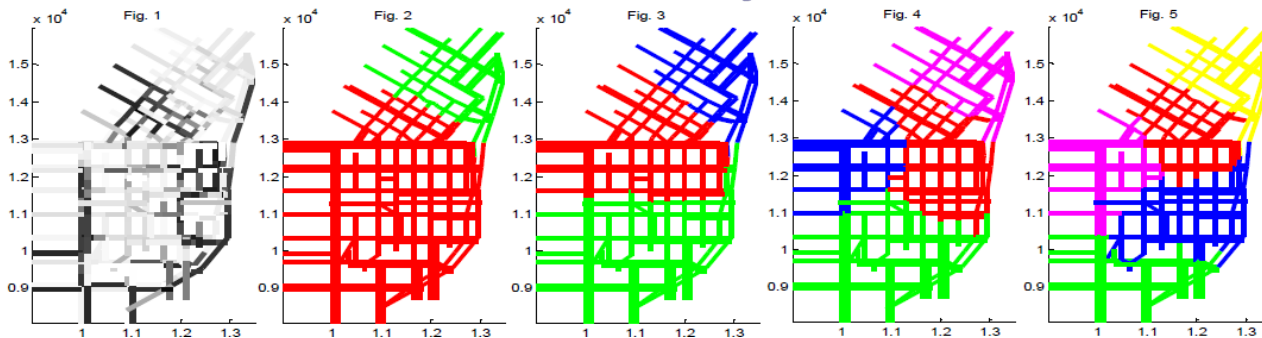
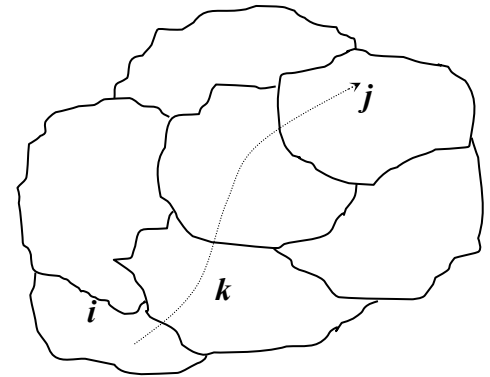
Solution (?):
A network based aggregated approach

“With four parameters I can fit an elephant, and with five I can make him wiggle his trunk”.

JOHN VON NEUMANN

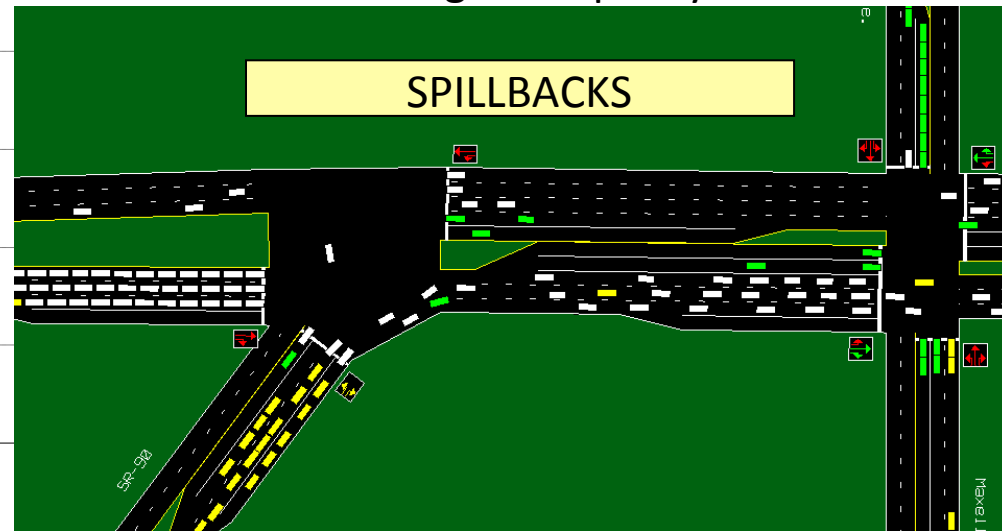
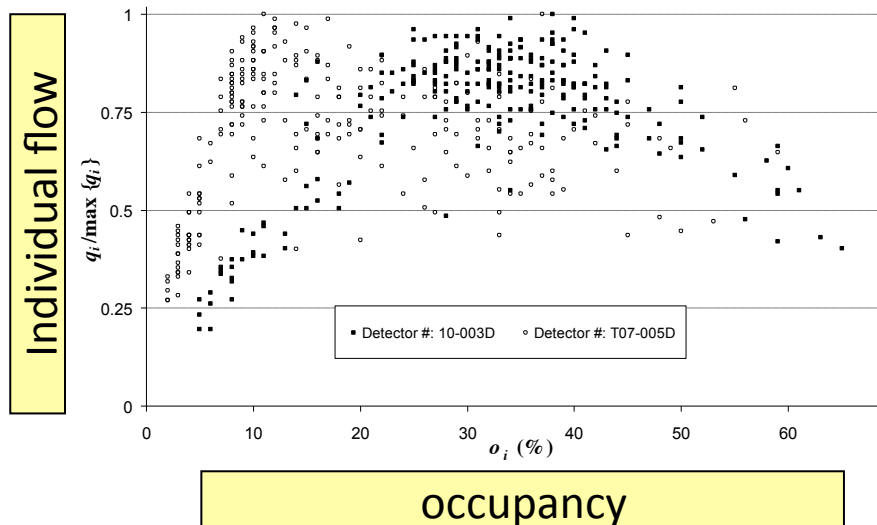
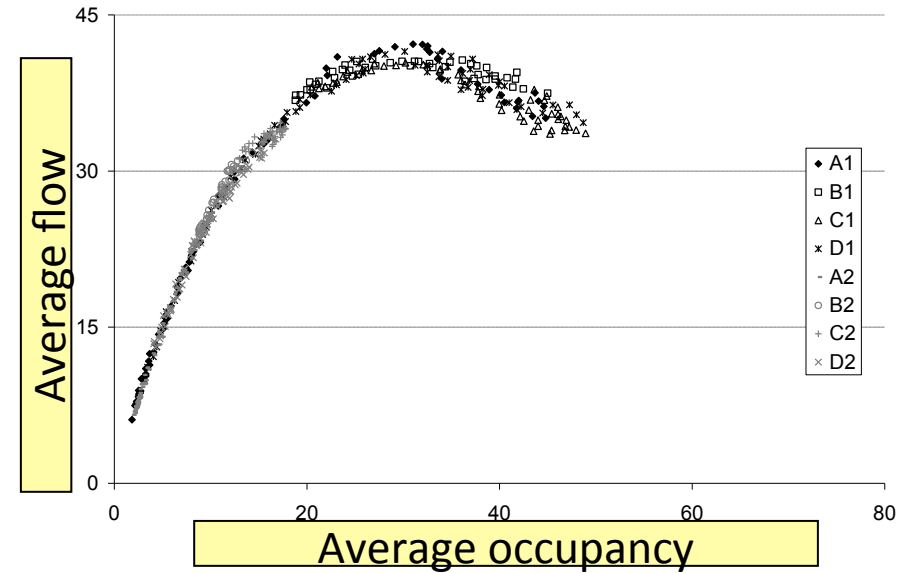
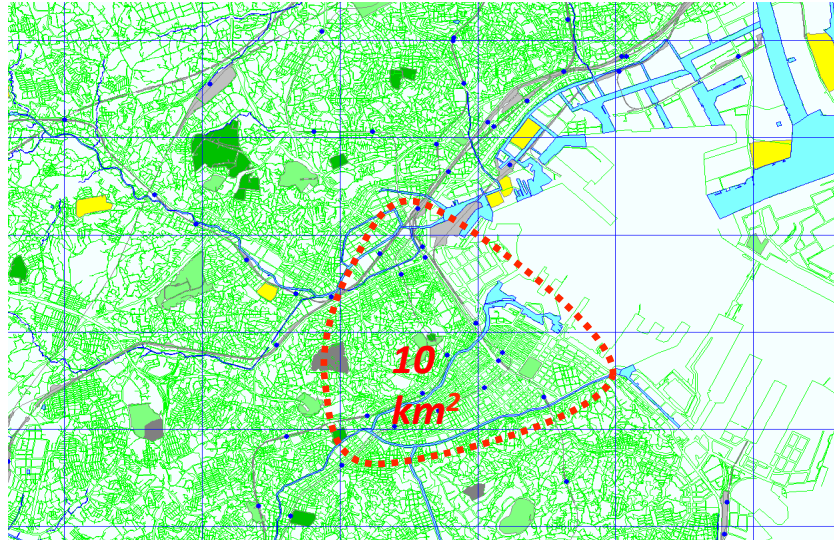
Challenges of spatial aggregation

- Physical Properties of aggregated models
- Macroscopic Fundamental Diagram (MFD)
- Partitioning (static, dynamic)
- Hierarchical control
- Multimodality



AGGREGATE BEHAVIOR
= ?
SCALED UP VERSION OF LINK BEHAVIOR

MFD Empirical results

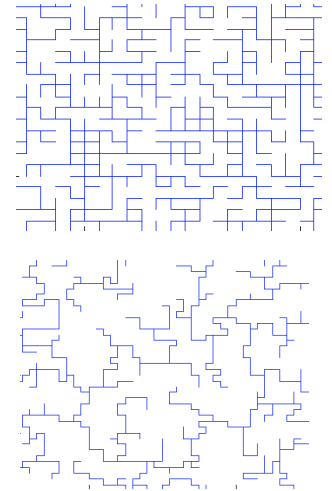


Network type and MFD

MFD IS NOT A UNIVERSAL LAW

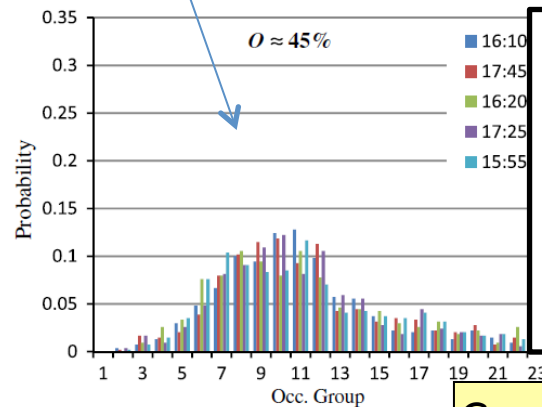
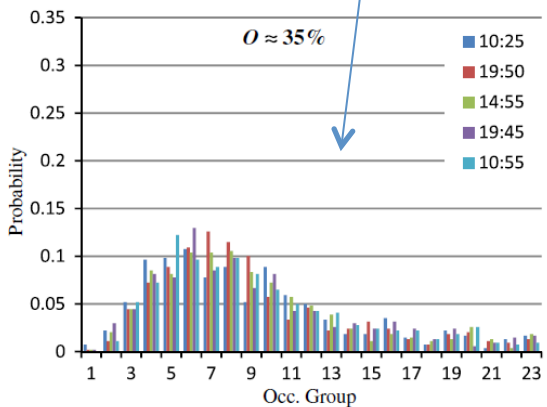
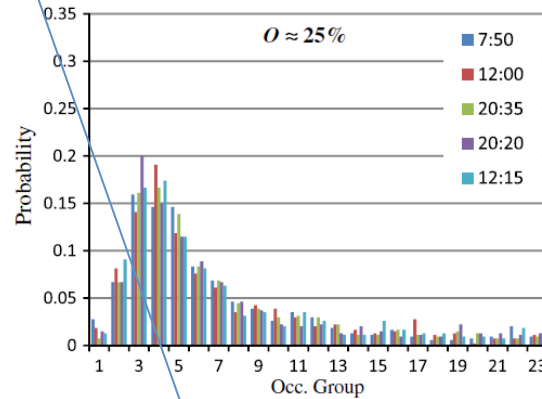
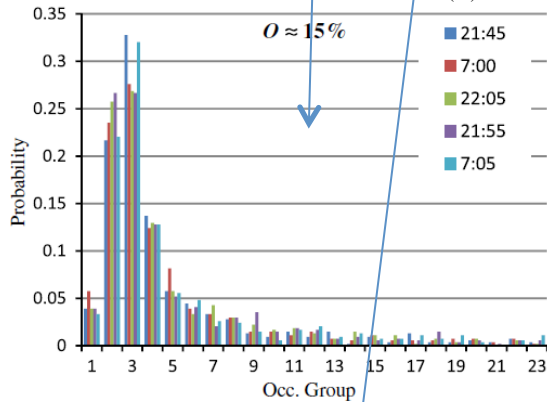
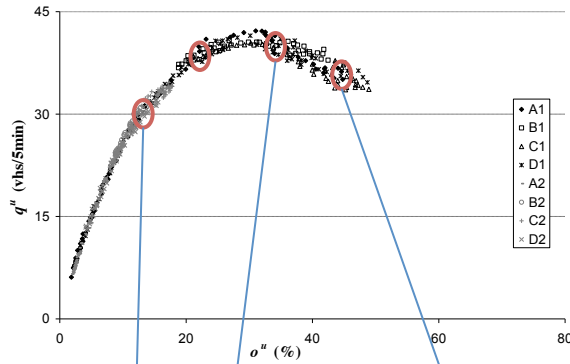
Regularity conditions that possibly ensure an MFD

- A slow-varying and distributed demand
- Homogeneous spatial distribution of congestion
- A redundant network with many route choices
- Homogeneity in network topology



-
- An MFD with low scatter
 - locally heterogeneous but macroscopically regular networks (e.g. cities with multiple modes)
 - An MFD with high scatter
 - Networks with uneven and inconsistent distribution of congestion (e.g. freeways)

Properties of a well-defined MFD



$d_r(t)$: pdf of individual detectors' density in region r
 $Q(t)$ and $O(t)$: Average network flow and density

$\{Q(t_1) = Q(t_2) \text{ and } O(t_1) = O(t_2)\}$

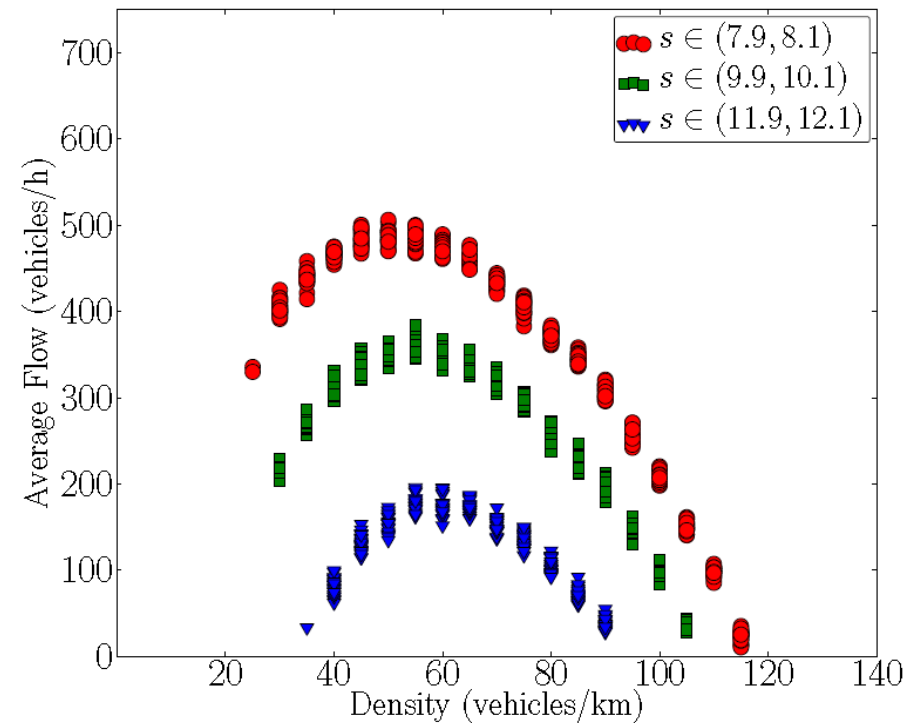
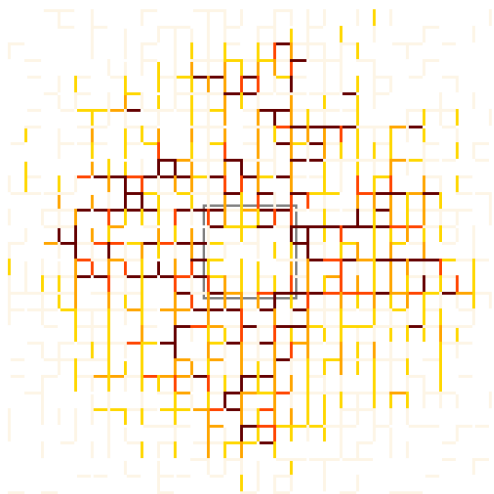
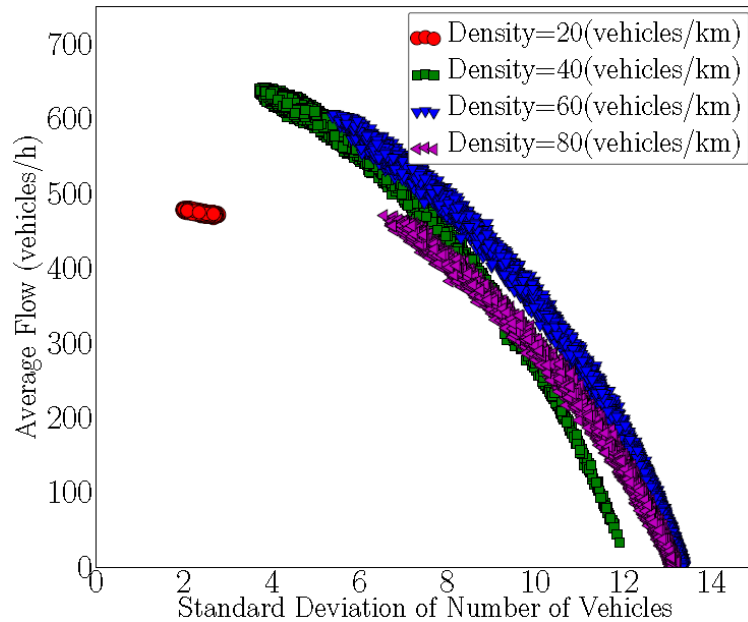
$\iff d_r(t_1) \sim d_r(t_2).$

Variance much higher than binomial's

WHY?

Correlation of link density (propagation)

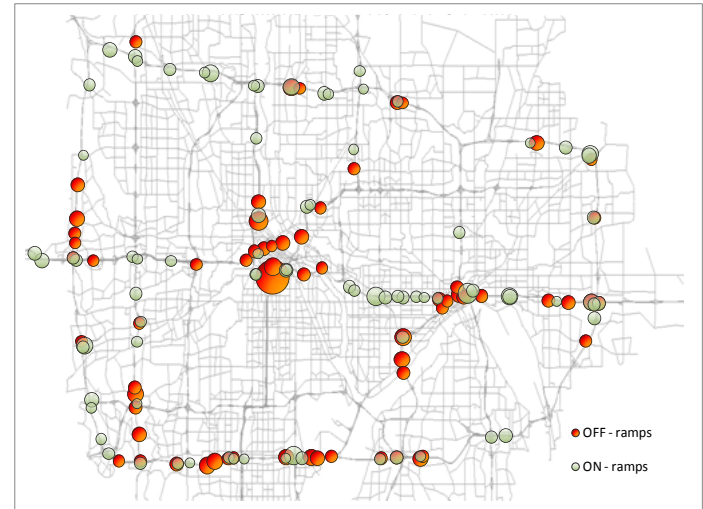
Spatial Variability and Network Capacity



Freeway MFDs (A “bad” example)

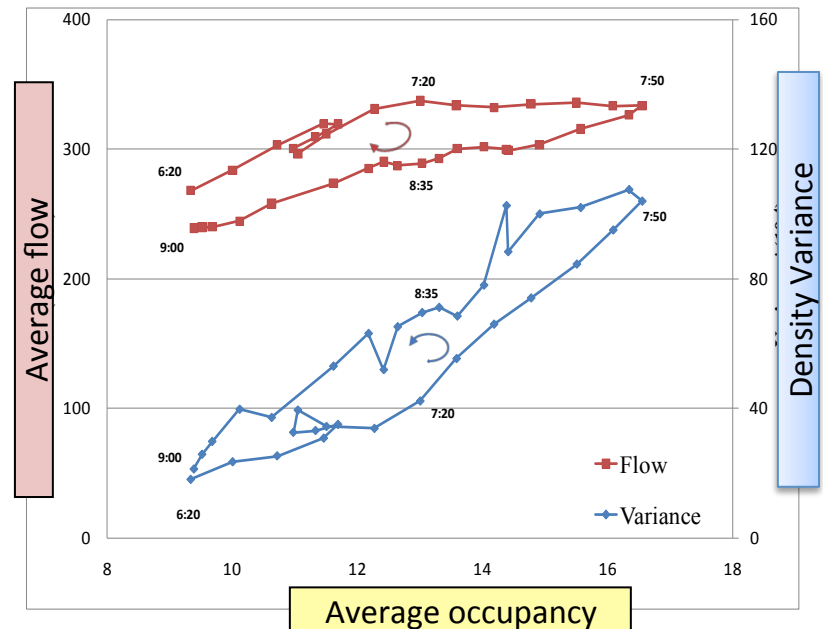
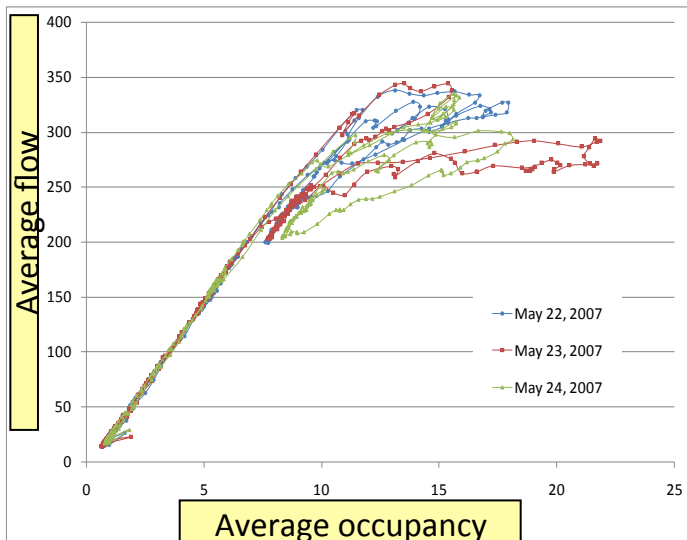
- Strong hysteresis phenomena in freeway MFDs

Freeway network of Minneapolis (USA)

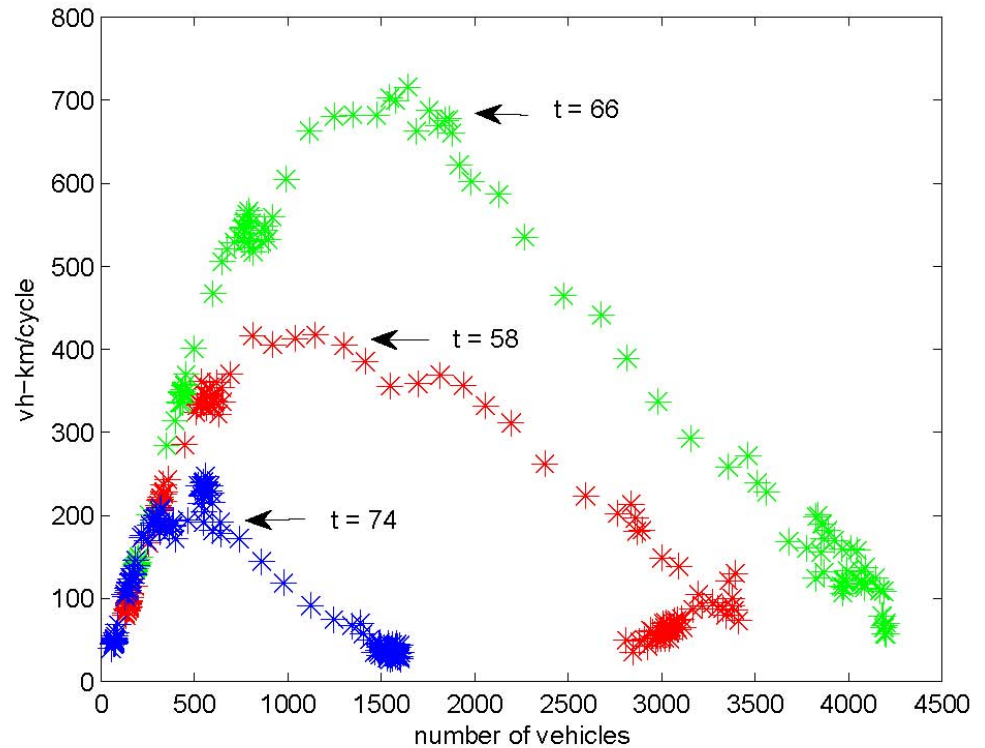
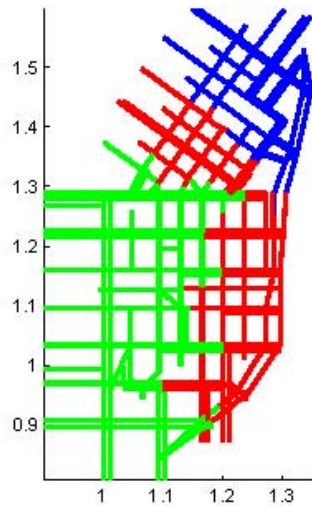


EXPLANATION

- Different distribution of congestion (onset vs. offset)



Congestion Spreading – Intro to Partitioning



Network static partitioning



Objectives

- Smooth boundaries (for control)
- Spatial Compactness
- Small heterogeneity within regions

1. Initialization (Ncut)
2. Merging
3. Boundary Adjustment (Fine tuning)

$$\text{Min } NS_k = \frac{\sum_{A \in C} NS_k(A)}{k}$$

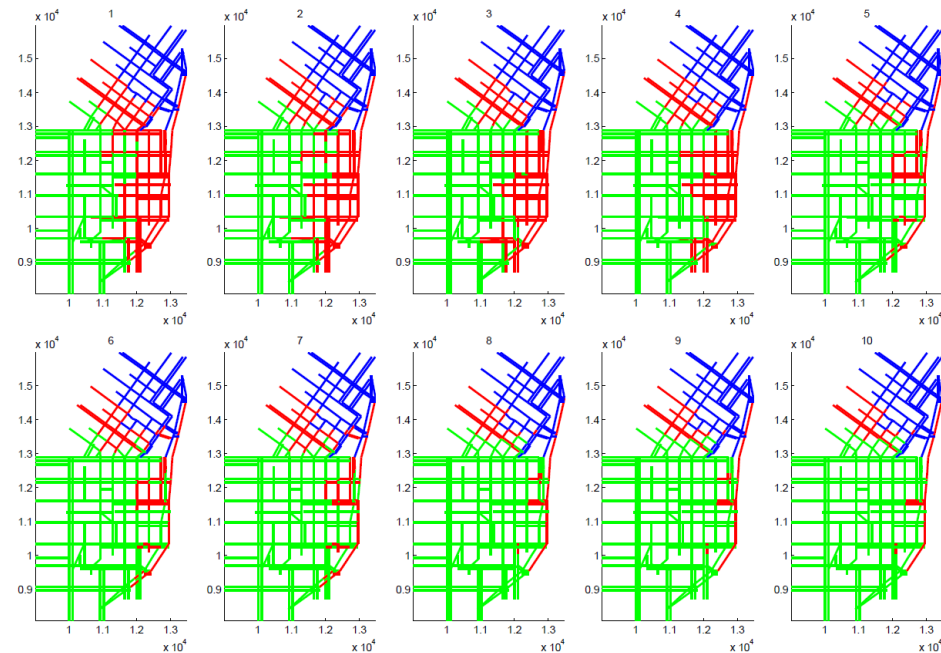
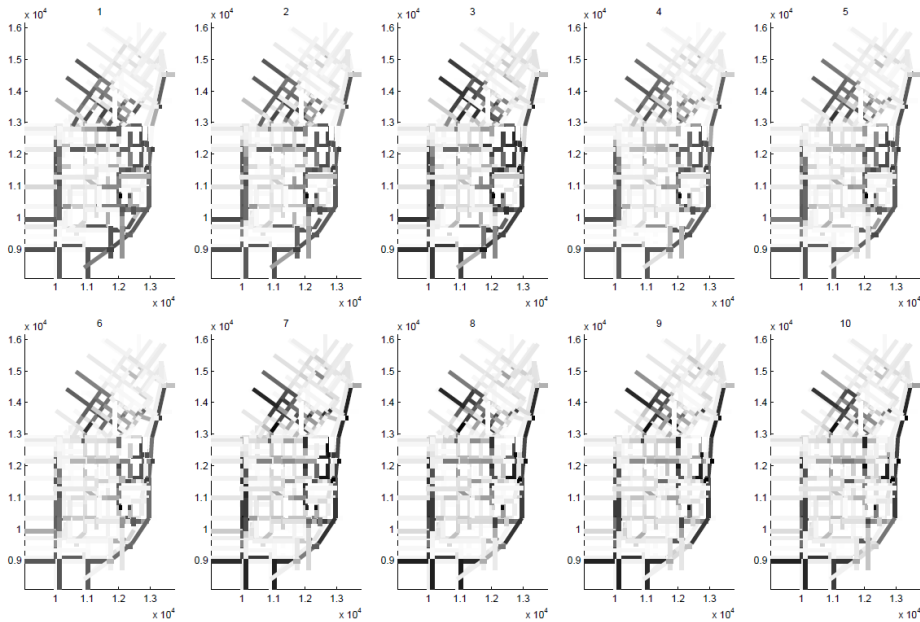
where

$$NS_k(A) = \frac{NS_k(A, A)}{NS_k(A, B)}$$

Intra-Similarity

Inter-Disimilarity

Congestion spreading identification

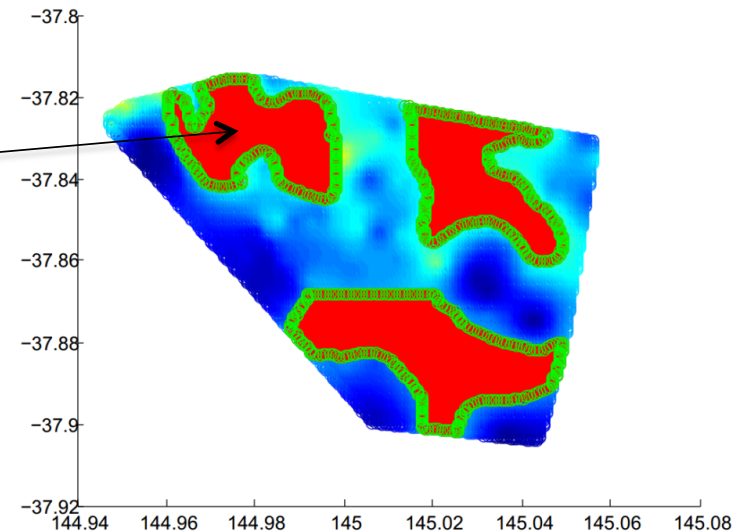
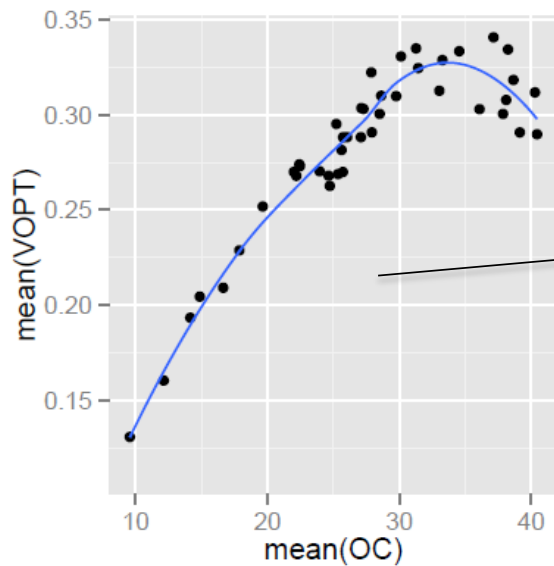
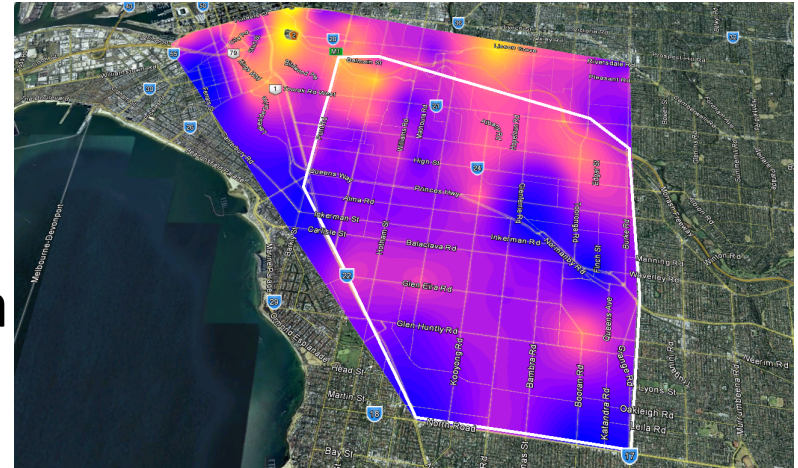


SIMPLE LOGIC

- Apply full algorithm at time $t=0$
- Apply only fine tuning for $t>0$
- New pockets of congestion are missing

Australian case study

- Melbourne Sydney
- Perimeter Control Case Study is prepared for beginning of 2014
- More than 5000 loop detector data



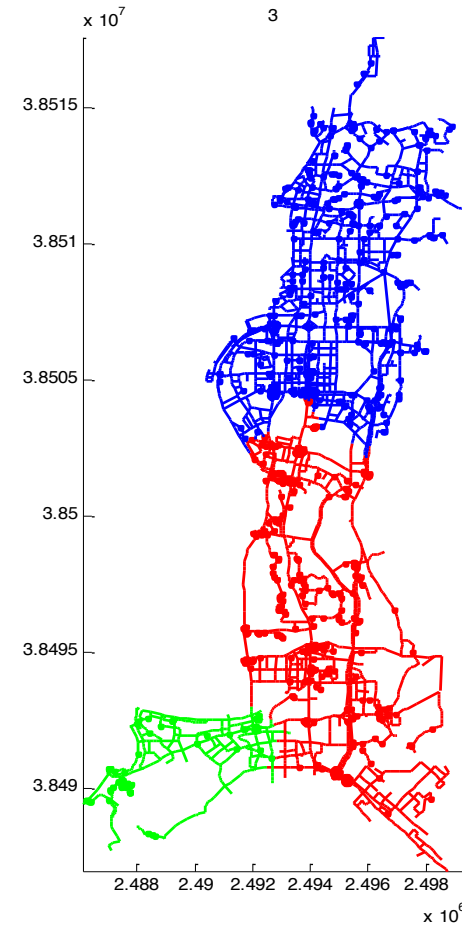
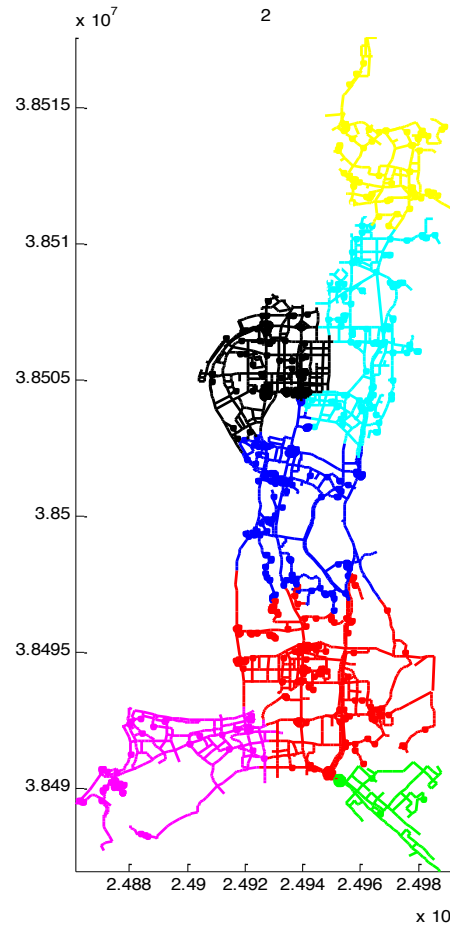
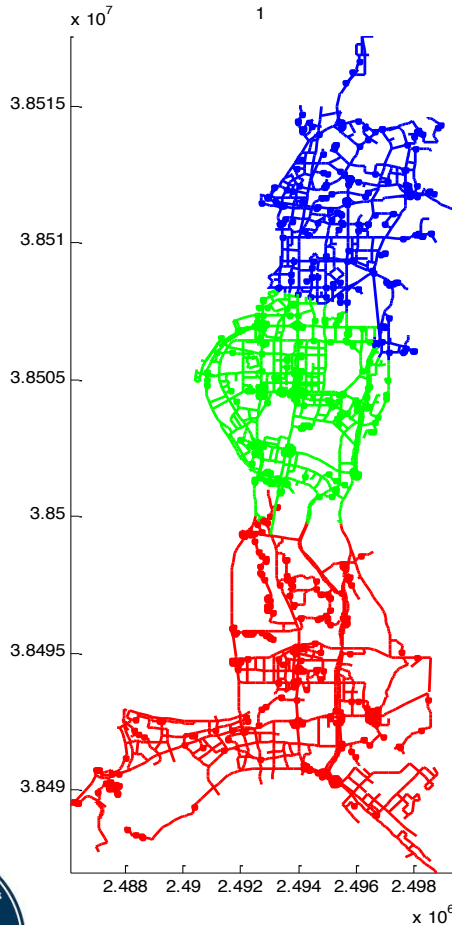
Dynamic Partitioning

Shenzhen case study

20000 taxis (25M points/day)

9000 links

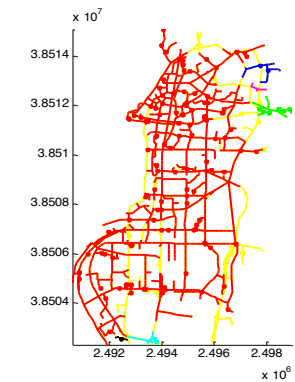
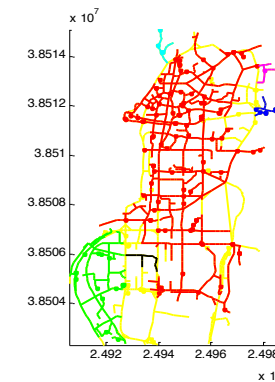
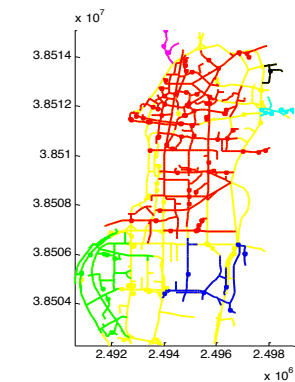
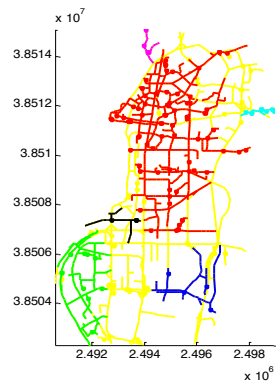
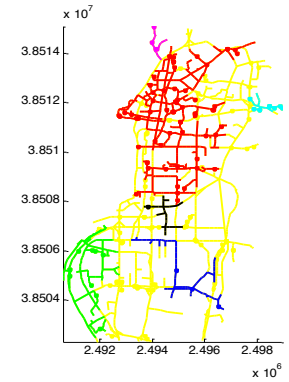
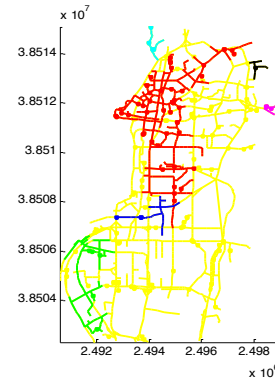
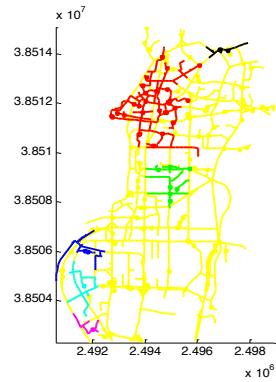
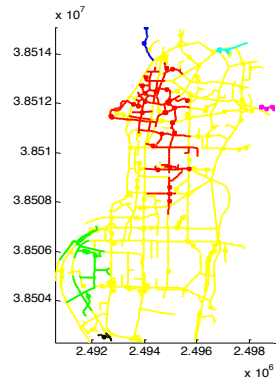
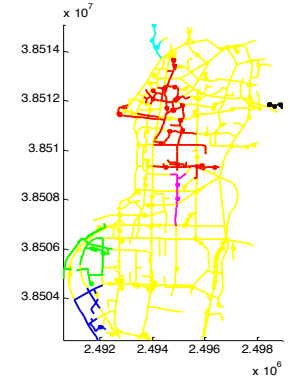
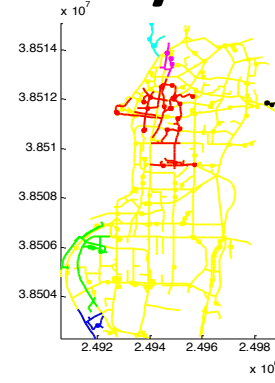
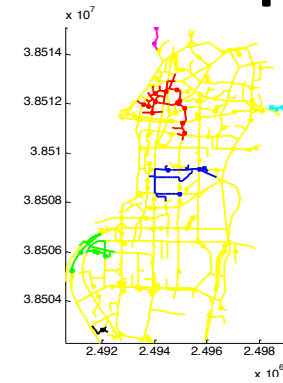
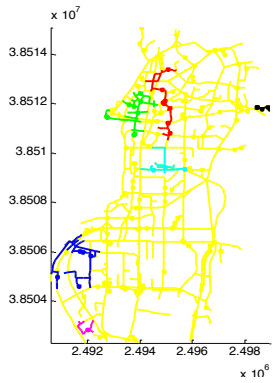
12M population



Ongoing

Ji and Geroliminis (2013) – Ongoing

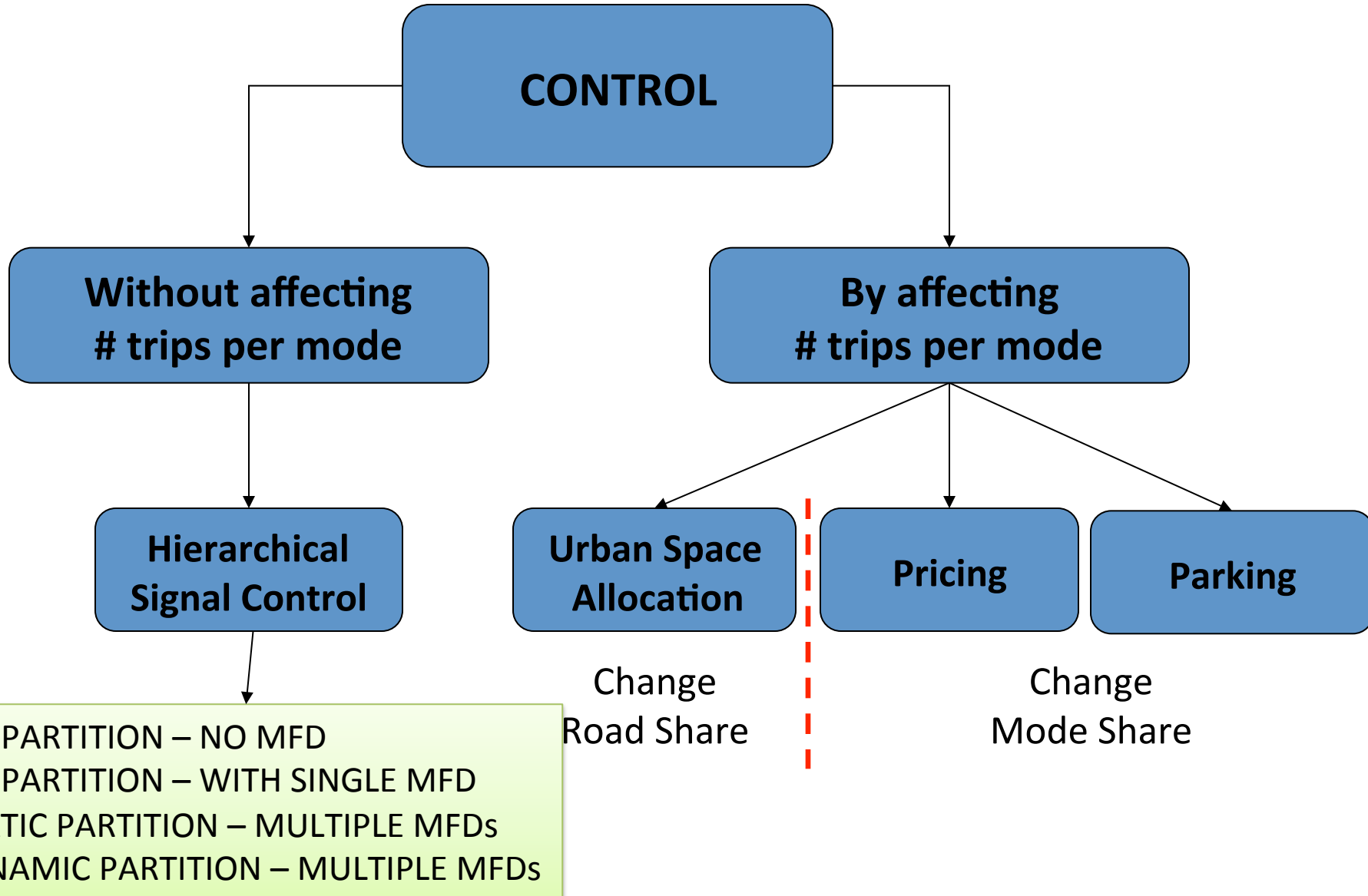
Spatiotemporal Dynamics



Small number of critical
pockets of congestion

20000 taxis (30M points/day)
9000 links
12M population

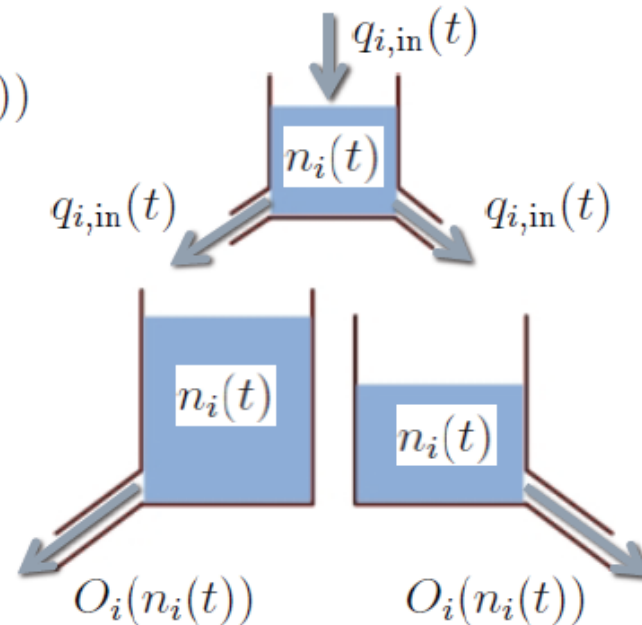
Smart Cities Management



Multivariable Feedback Regulators

- **Given:** MFDs for each reservoir $O_i(n_i(t))$
- **Observe:** Accumulation $n_i(t)$
- **Control:** Input $q_{i,in}(t)$
- **Maximize:** Throughput
- **Minimize:** Risk overflow
- **Nonlinear Dynamics**

$$\frac{dn_i(t)}{dt} = q_{i,in}(t) - q_{i,out}(t) + d_i(t)$$



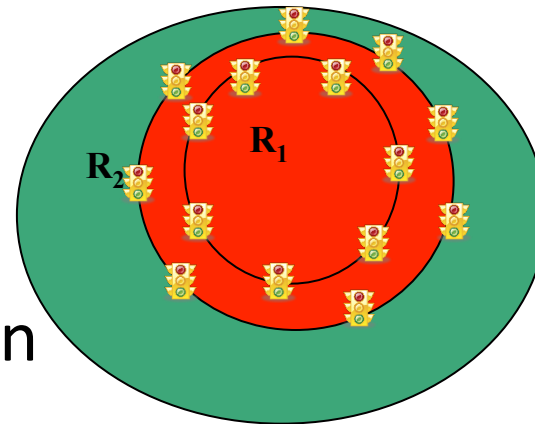
- **Linear-quadratic control** (multivariable P-regulators)

$$\beta(k) = \hat{\beta} - \mathbf{K} [\mathbf{n}(k) - \hat{\mathbf{n}}]$$
- **Linear-quadratic-integral control** (multivariable PI-regulators)

$$\beta(k) = \beta(k - 1) - \mathbf{K}_p [\mathbf{n}(k) - \mathbf{n}(k - 1)] - \mathbf{K}_I [\mathbf{n}(k) - \hat{\mathbf{n}}]$$

Selection of perimeter

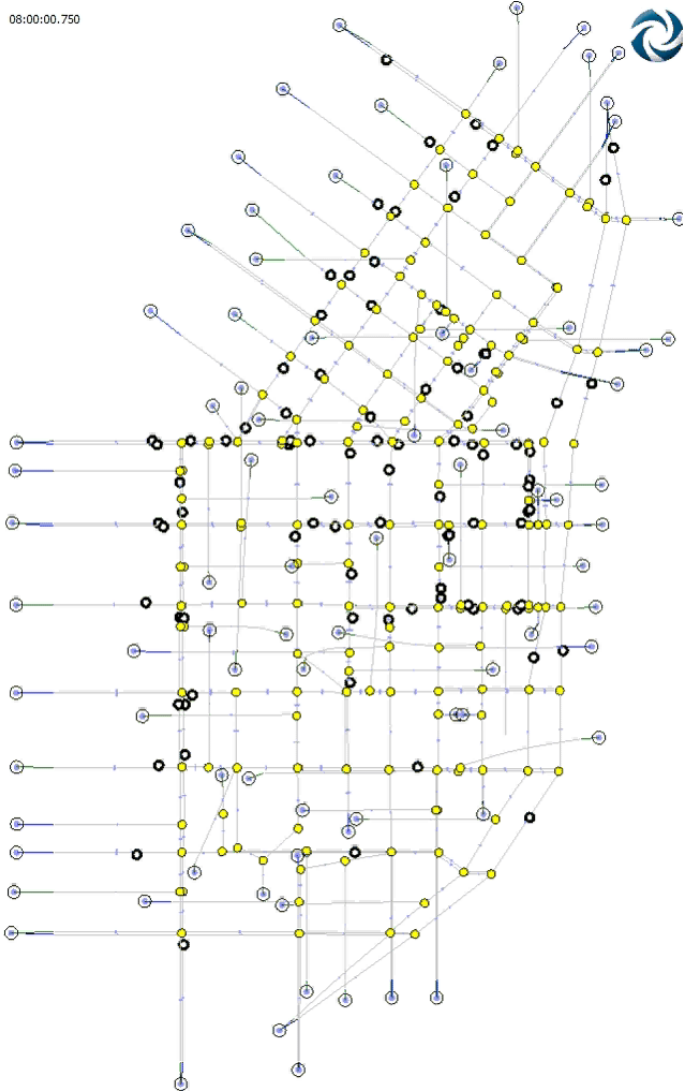
- Criteria
 - Partitioning (Region Homogeneity)
 - Critical traffic signals (underutilization of green)
 - Queue lengths propagation
 - Adaptivity
- Implementation
 - Queue length equalization
 - Equity



Feedback Multi-Boundary Control

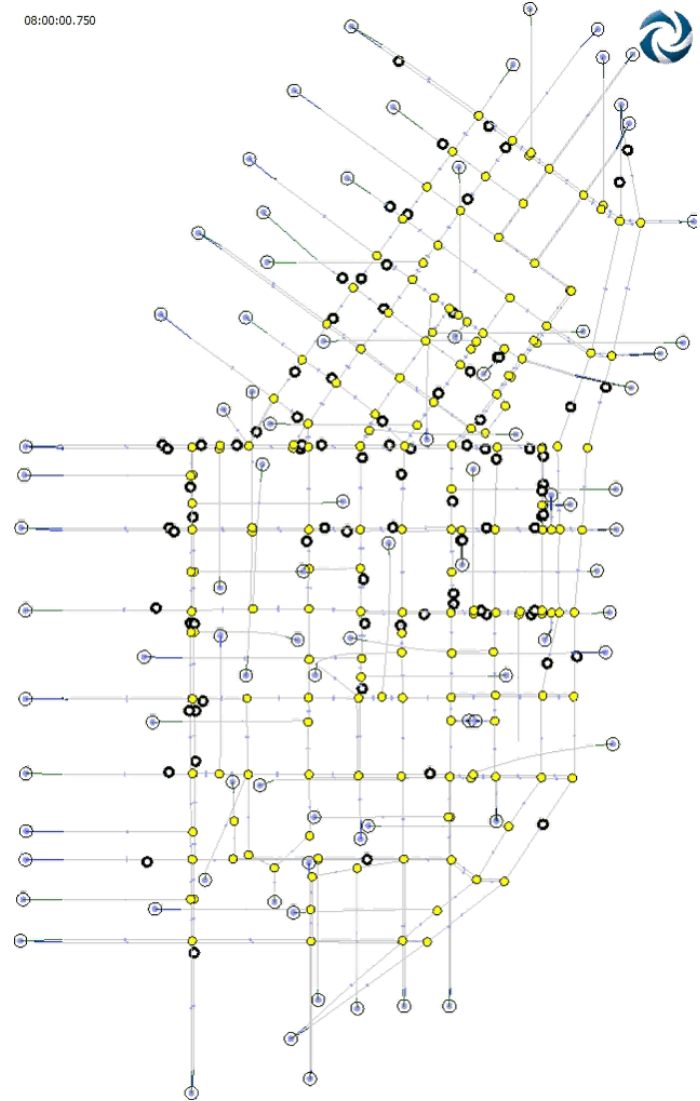
Pre-timed Traffic Control

08:00:00.750

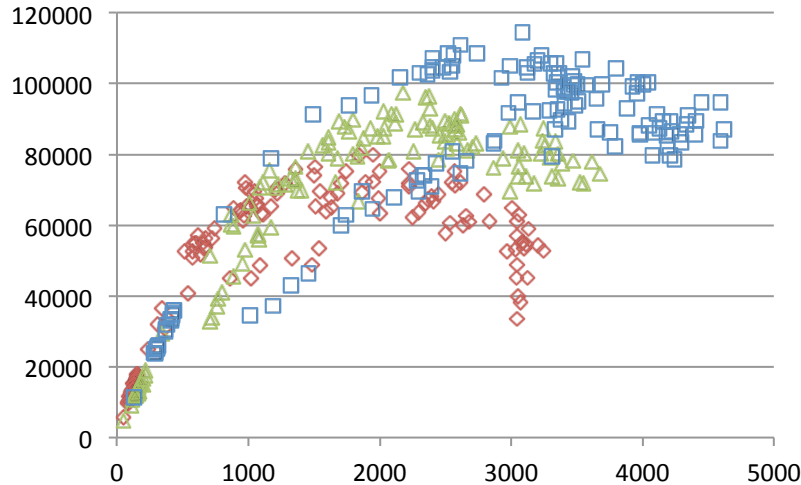


Smart Traffic Control

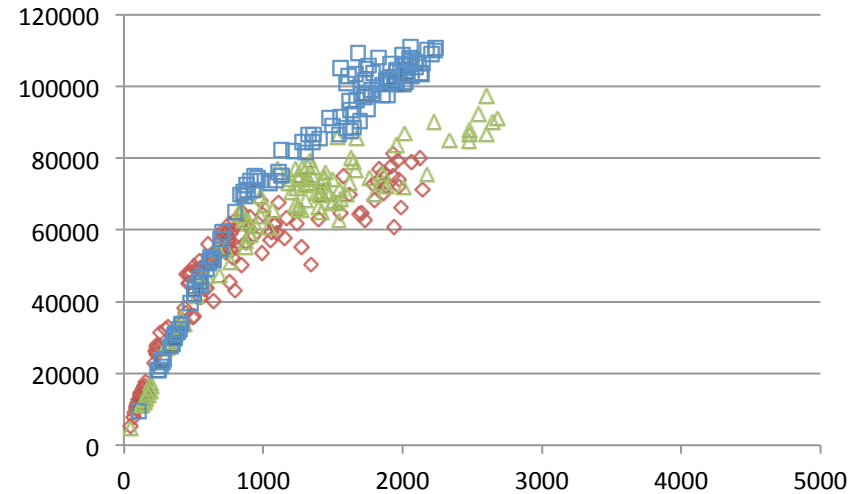
08:00:00.750



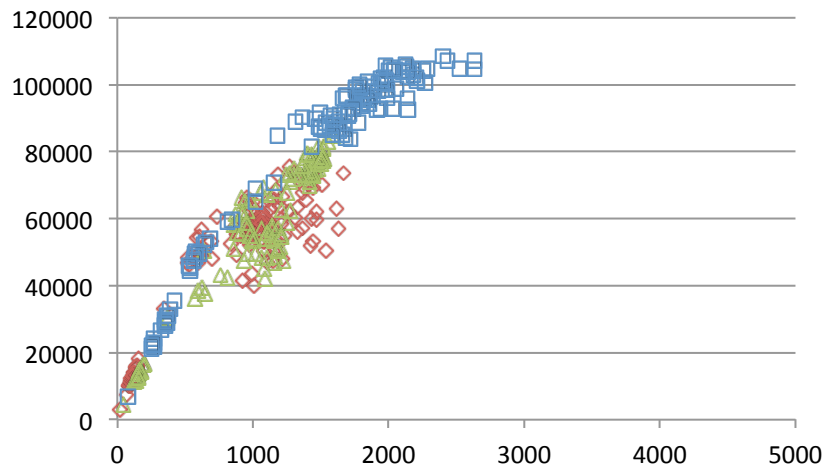
Comparison with Other Controllers



Pre-timed fixed control (PT)



Multiple MFDs perimeter + boundary controllers (NEW)



1 MFD perimeter controller (BBC)

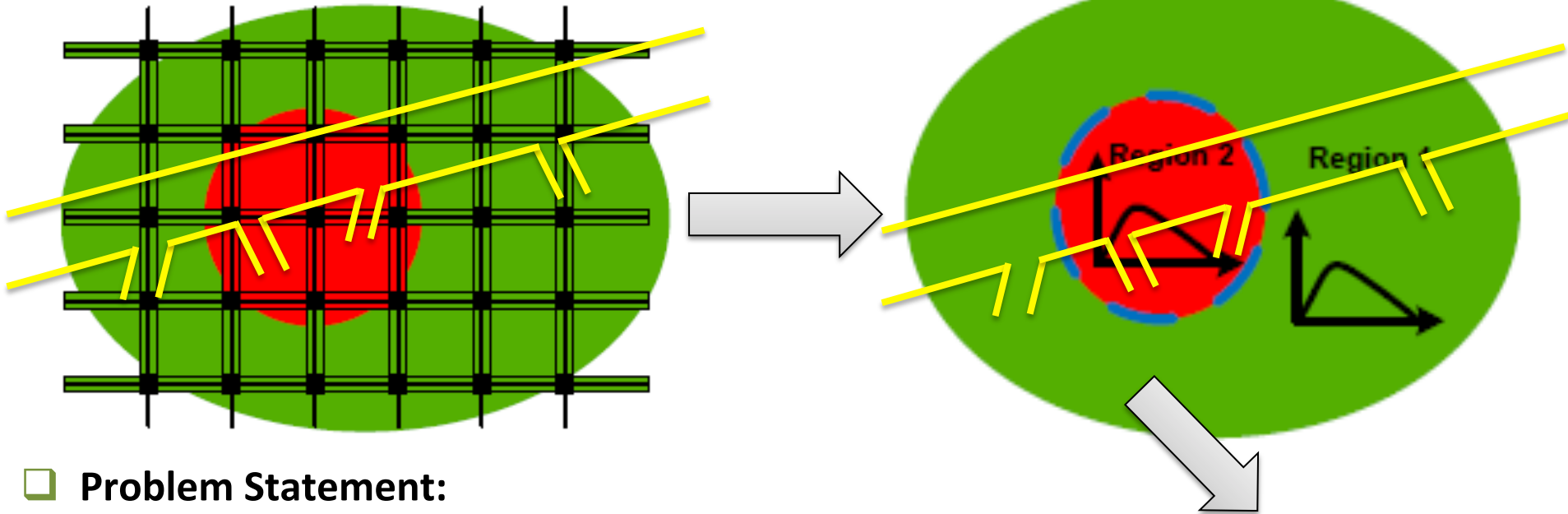
Improvements (total travel time)

- PT vs. NEW 45%
- NEW vs. BBC 12%

- Equitable distribution of queues
- Earlier activation of Control

Mixed Freeway-Arterial network

uneven distribution of congestion

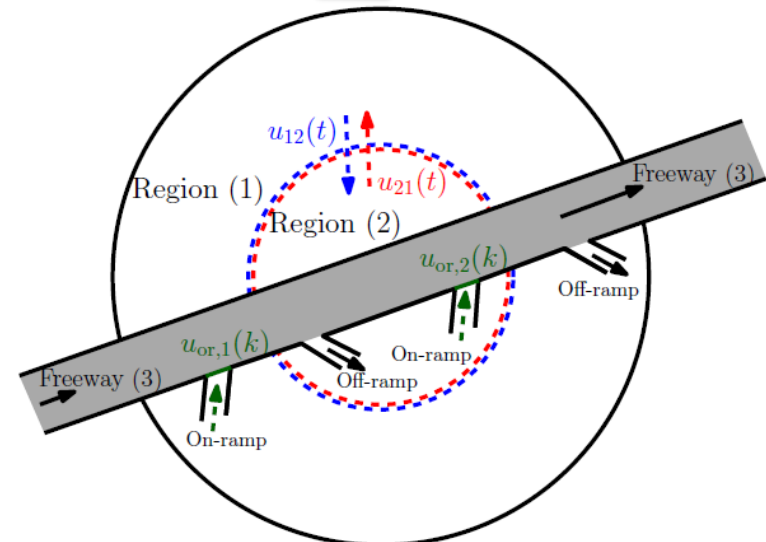


□ Problem Statement:

- Coordinated control of a mixed traffic network
- The goal is to minimize the network total delay
- A receding horizon framework (MPC) to solve the optimal control problem

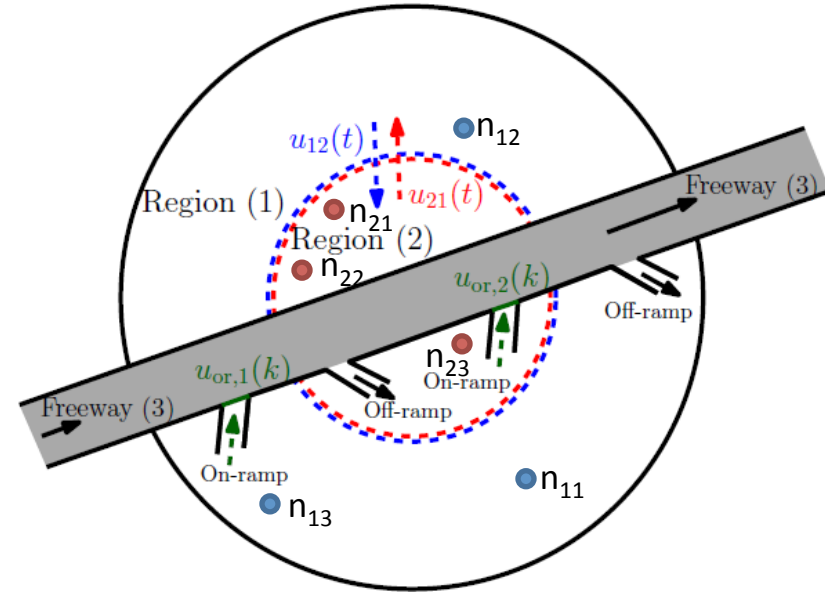
□ Controllers are:

- 2 Ramp metering
- 2 Perimeter controllers

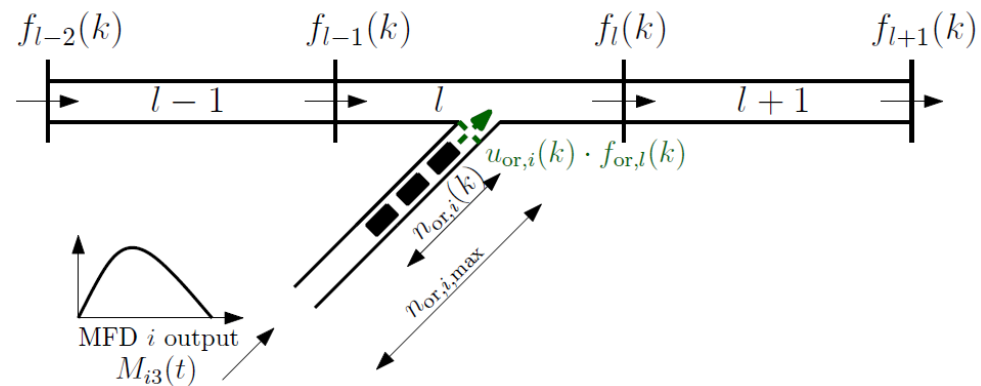


Problem Definition

- The urban regions are modeled with MFDs
- The traffic dynamics of the freeway are modeled with the cell transmission model (CTM)
- Dynamic trip route choice
- Time dependent O-Ds



O \ D	1	2	3
1	$q_{11} : 1 \rightarrow 1$ $q_{131} : 1 \rightarrow 3 \rightarrow 1$	$q_{12} : 1 \rightarrow 2$ $q_{132} : 1 \rightarrow 3 \rightarrow 2$	$q_{13} : 1 \rightarrow 3$ $q_{123} : 1 \rightarrow 2 \rightarrow 3$
2	$q_{21} : 2 \rightarrow 1$ $q_{231} : 2 \rightarrow 3 \rightarrow 1$	$q_{22} : 2 \rightarrow 2$	$q_{23} : 2 \rightarrow 3$ $q_{213} : 2 \rightarrow 1 \rightarrow 3$
3	$q_{31} : 3 \rightarrow 1$ $q_{321} : 3 \rightarrow 2 \rightarrow 1$	$q_{32} : 3 \rightarrow 2$ $q_{312} : 3 \rightarrow 1 \rightarrow 2$	$q_{33} : 3 \rightarrow 3$



Problem Formulation

$$J = \min_{\substack{u_{12}(t), u_{21}(t) \\ u_{or,1}(k), u_{or,2}(k)}} \int_{t_0}^{t_f} [n_1(t) + n_2(t)] dt + \sum_{k=0}^{K-1} \sum_{l=1}^L x_l(k)$$

$$\diamond M_{ij} = \frac{n_{ij}}{n_i} \times G_i(n_i(t))$$

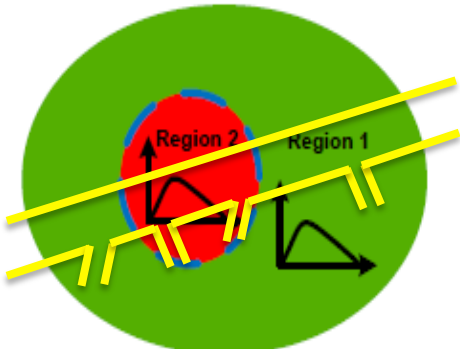
Subject to:

- $\frac{dn_{11}(t)}{dt} = \frac{\hat{q}_{321}(t) + q_{23}(t)}{\hat{q}_{321}(t) + q_{213}(t) + q_{21}(t)} u_{21}(t) \cdot M_{21}(t) + q_{11}(t) + \hat{q}_{231}(t) + \hat{q}_{31}(t) - M_{11}(t)$
- $\frac{dn_{12}(t)}{dt} = q_{12}(t) + q_{123}(t) + \hat{q}_{312}(t) - u_{12}(t) \cdot M_{12}(t)$
- $\frac{dn_{13}(t)}{dt} = \frac{q_{213}(t)}{\hat{q}_{321}(t) + q_{213}(t) + q_{21}(t)} u_{21}(t) \cdot M_{21}(t) + q_{13}(t) + q_{131}(t) + q_{132}(t) - \min(M_{13}(t), C_{or,1}(t))$
- $\frac{dn_{21}(t)}{dt} = q_{21}(t) + q_{213}(t) + \hat{q}_{321}(t) - u_{21}(t) \cdot M_{21}(t)$
- $\frac{dn_{22}(t)}{dt} = \frac{\hat{q}_{312}(t) + q_{12}(t)}{\hat{q}_{312}(t) + q_{12}(t) + q_{123}(t)} u_{12}(t) \cdot M_{12}(t) + q_{22}(t) + \hat{q}_{132}(t) + \hat{q}_{32}(t) - M_{22}(t)$
- $\frac{dn_{23}(t)}{dt} = \frac{q_{123}(t)}{\hat{q}_{312}(t) + q_{12}(t) + q_{123}(t)} u_{12}(t) \cdot M_{12}(t) + q_{23}(t) + q_{231}(t) - \min(M_{23}(t), C_{or,2}(t))$
- $C_{or,i}(t) = (n_{or,i,max} - n_{or,i}(k)) / T_k$; available flow capacity in the on-ramp queue
- $u_{min} \leq u_{12}(t), u_{21}(t) \leq u_{max}$; $u_{min} \leq u_{or,1}(k), u_{or,2}(k) \leq u_{max}$
- $0 \leq n_1(t) \leq n_{1,jam}$; $n_1(t) = n_{11}(t) + n_{12}(t) + n_{13}(t)$
- $0 \leq n_2(t) \leq n_{2,jam}$; $n_2(t) = n_{21}(t) + n_{22}(t) + n_{23}(t)$
- and CTM formulas

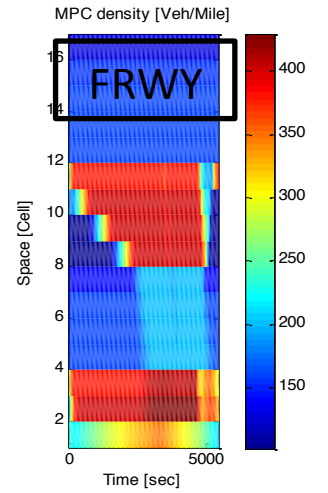
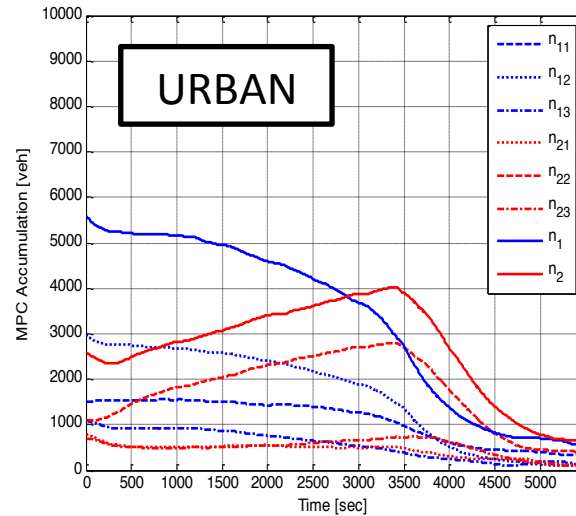
Results

Delay (veh.sec X 10⁶)

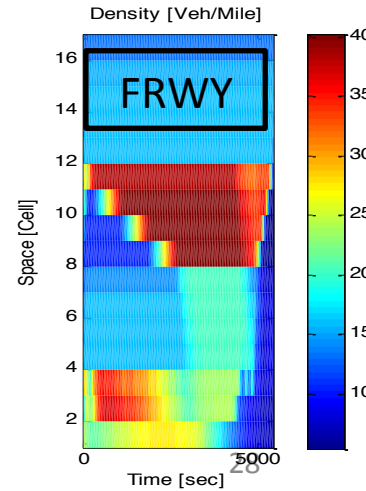
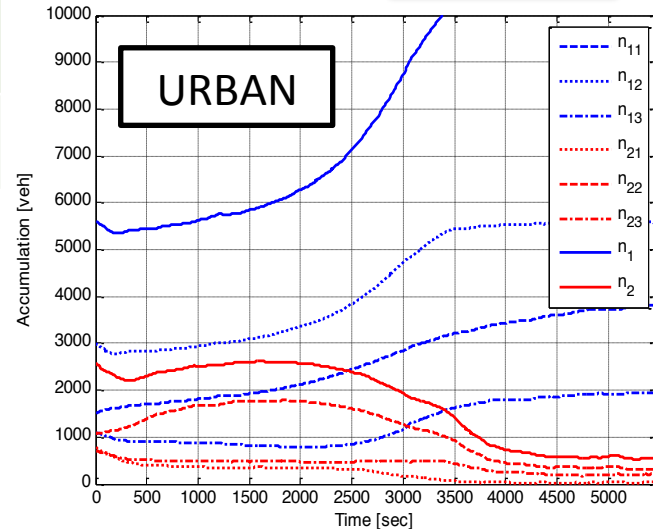
	ALINEA Q	Urban MPC + ALINEA Q	FULL MPC
Region 1	438	262	196
Region 2	97	160	143
Freeway	172	189	218
On-Ramp 1	13	15	8
On-Ramp 2	16	16	16
Network	736	642	581



FULL MPC



ALINEA Q



Multimodal networks

- In urban networks, buses usually share the same network with the other vehicles.
- Movement Conflicts in multi-modal urban traffic systems
- Bus stops affect the system like variable red signals in a single lane (instead of blocking all lanes).
- Increasing bus frequency decreases the flow of vehicles but can increase the flow of passengers.



Performance Measures

Vehicle Hours Traveled
Vehicle Kilometers Traveled

Passenger Hours Traveled
Passenger Kilometers Traveled

Mobility (Accessibility)

Emissions (Environ. Impacts)

Costs (Users, Providers, etc.)

Road Space Used

- **Competing modes**
- **Parking**
- **Pax vs. veh throughput**

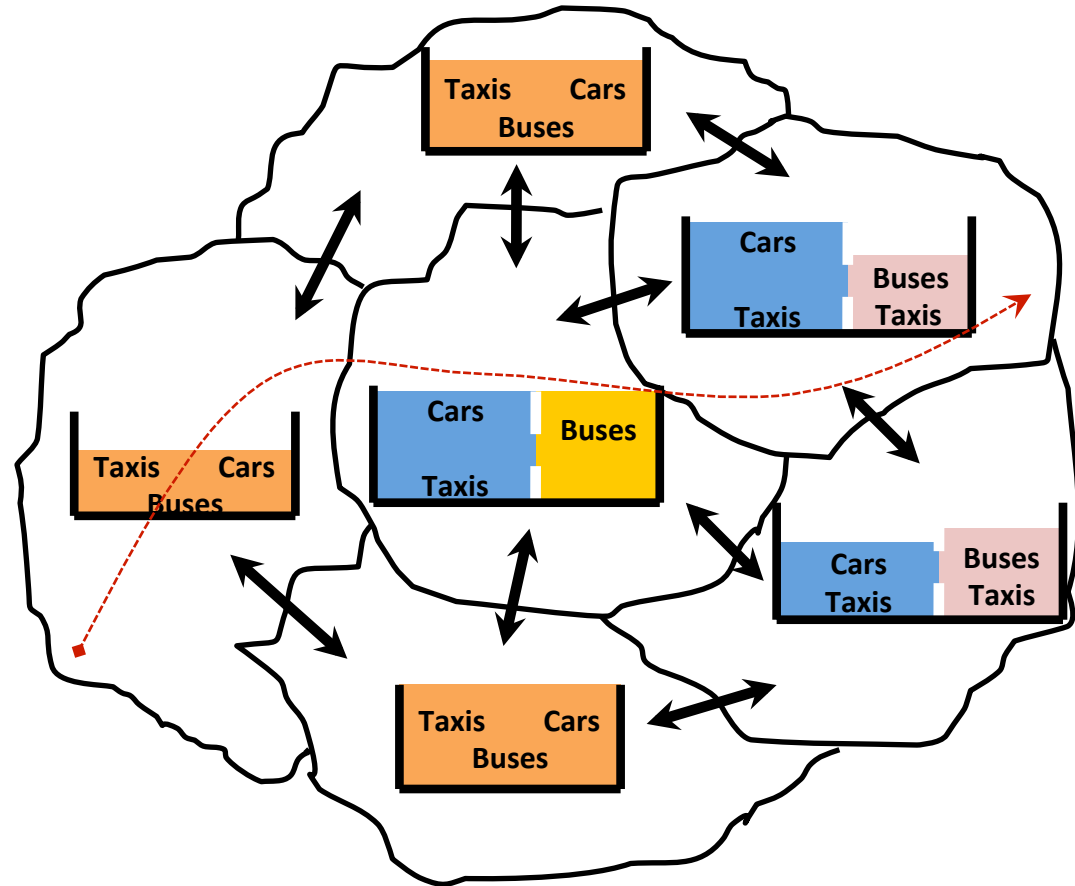
MULTIMODAL CITIES

Multimodal multi-reservoir system



Challenges

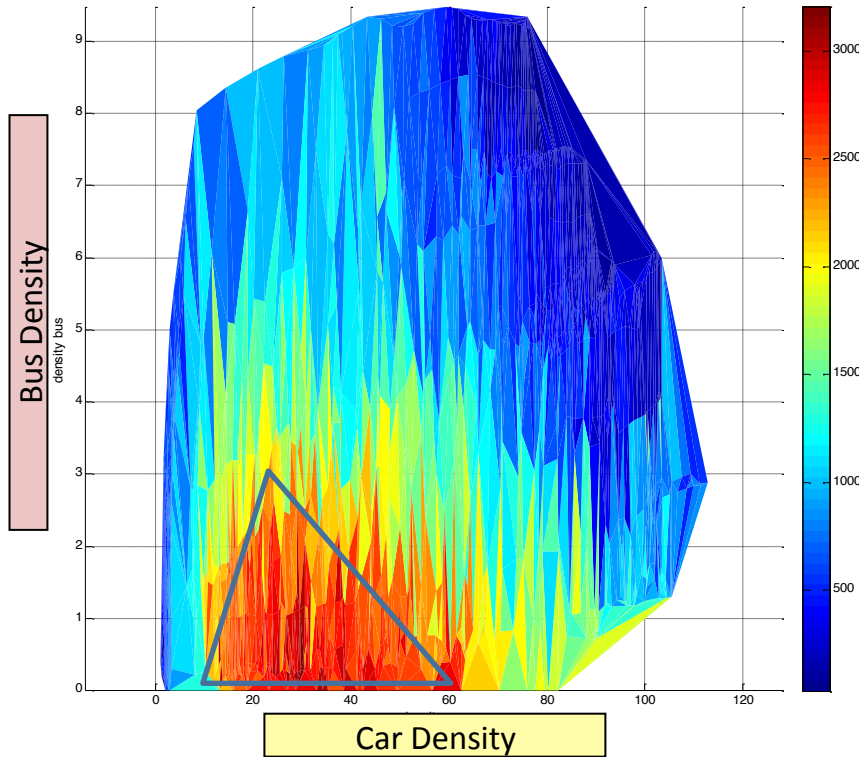
- Model: Dynamics
- Monitor: Existence + Observability
- Control: Redistribution of urban space between modes
- Implementation



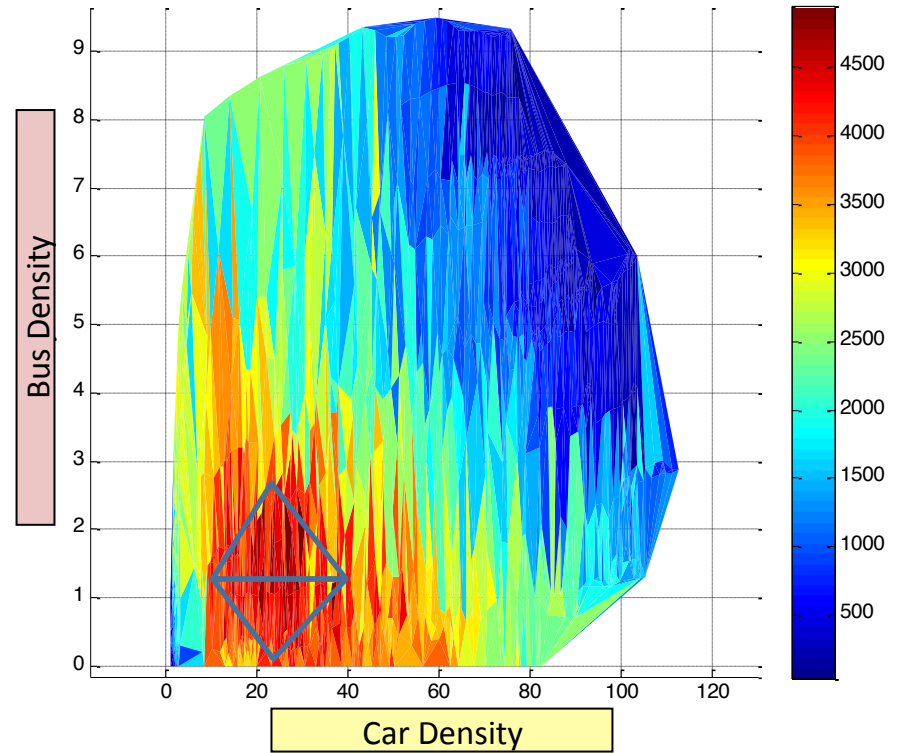
Geroliminis and Boyaci (2012) – Tr. Res. Part B

Zheng and Geroliminis (2013) ISTTT20

Two-mode 3-D MFD (mixed traffic)



VEHICULAR FLOW



PASSENGER FLOW

Simulated data – Downtown SF

Challenging Research Questions

- Control of more complex city structures with route choice
- Field test Implementations
- Congestion Spreading in 2D urban networks
- Travel time reliability and Control
- Multimodal city networks (People + Goods)
- Smart shared-use mobility



Vietnam



United Kingdom



DISCUSSION

