

# Kinetic modeling and Metabolic Control Analysis to understand the control and regulation of metabolic pathways

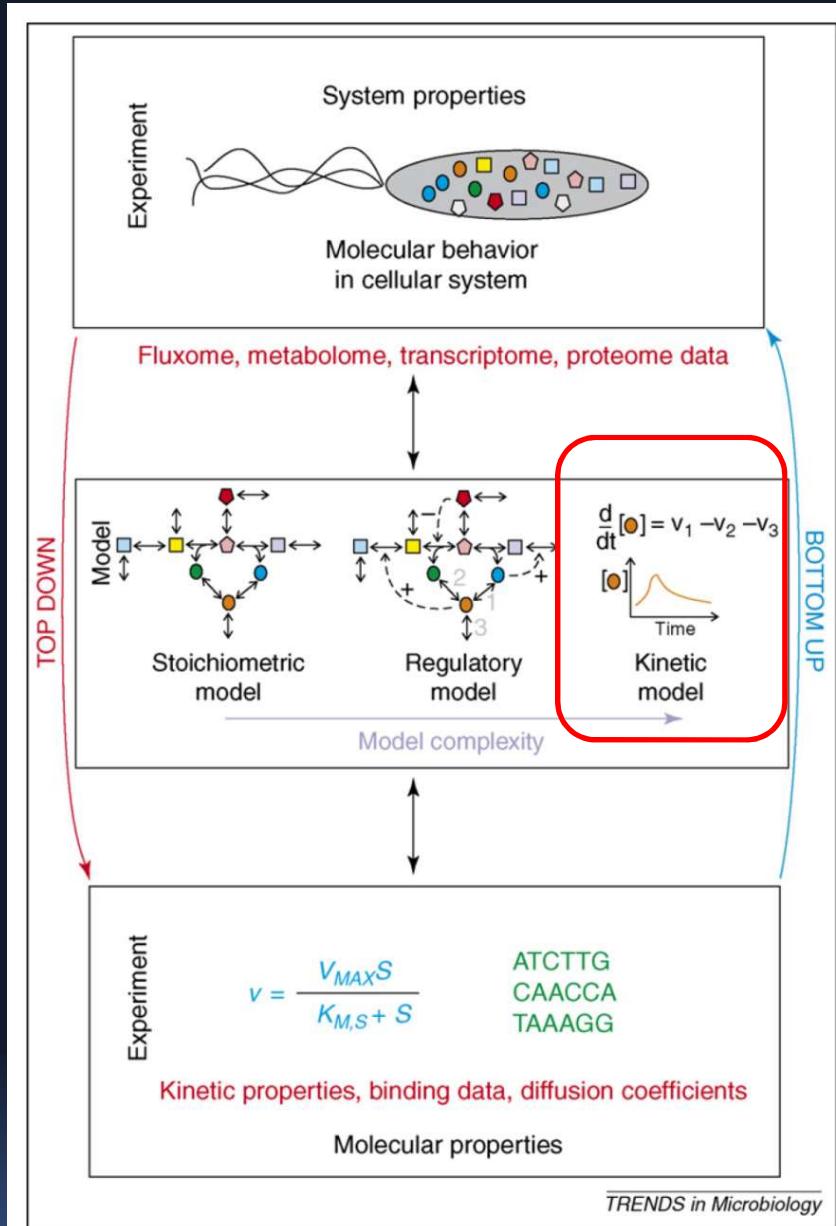
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# Systems Biology aim: to build computational models of complex cellular networks

## Top-Down strategy

- Uses high-throughput “omic” data.
- Describes behavior patterns and cause-effect relationships of macromolecules.



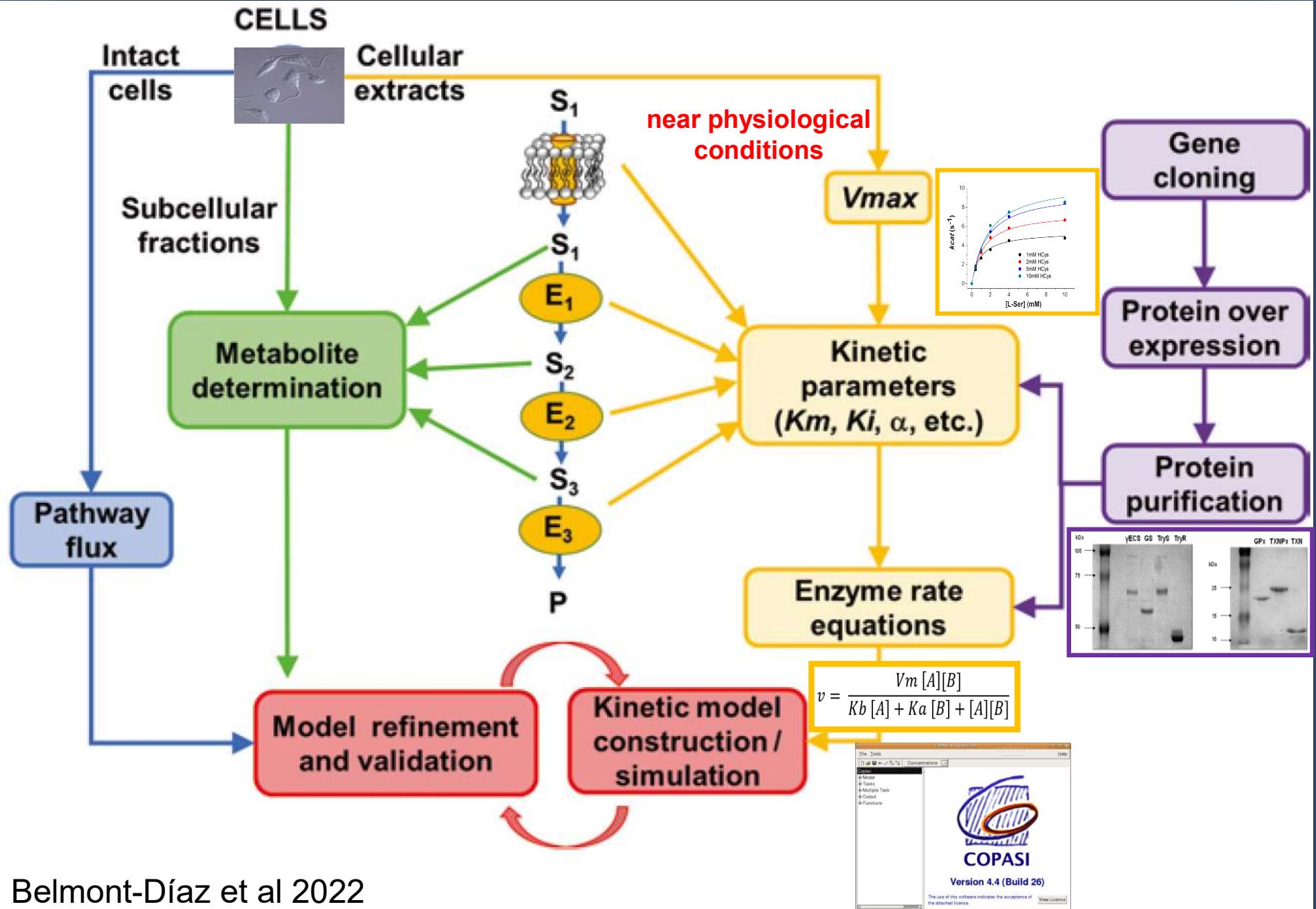
## Bottom-Up (kinetic modeling)

- Based on the kinetic properties from the individual enzymes, thermodynamic parameters

- Allow to elucidate the underlying controlling and regulatory mechanisms

Bruggeman & Westerhoff 2006  
Trends Microbiol

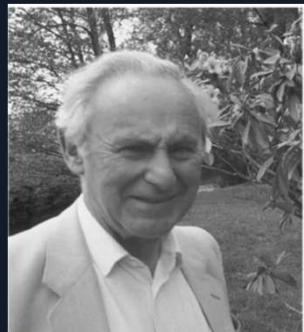
## What is needed to build a kinetic model of a metabolic pathway?



Belmont-Díaz et al 2022

# What is Metabolic Control Analysis?

- Henrik Kacser and James A Burns (Edinburgh, Scotland) 1973
- Reinhart Heinrich and Tom Rapoport (Berlin, Germany) 1973



- Molecular basis of dominance
- Mathematical modeling of glycolysis in erythrocytes

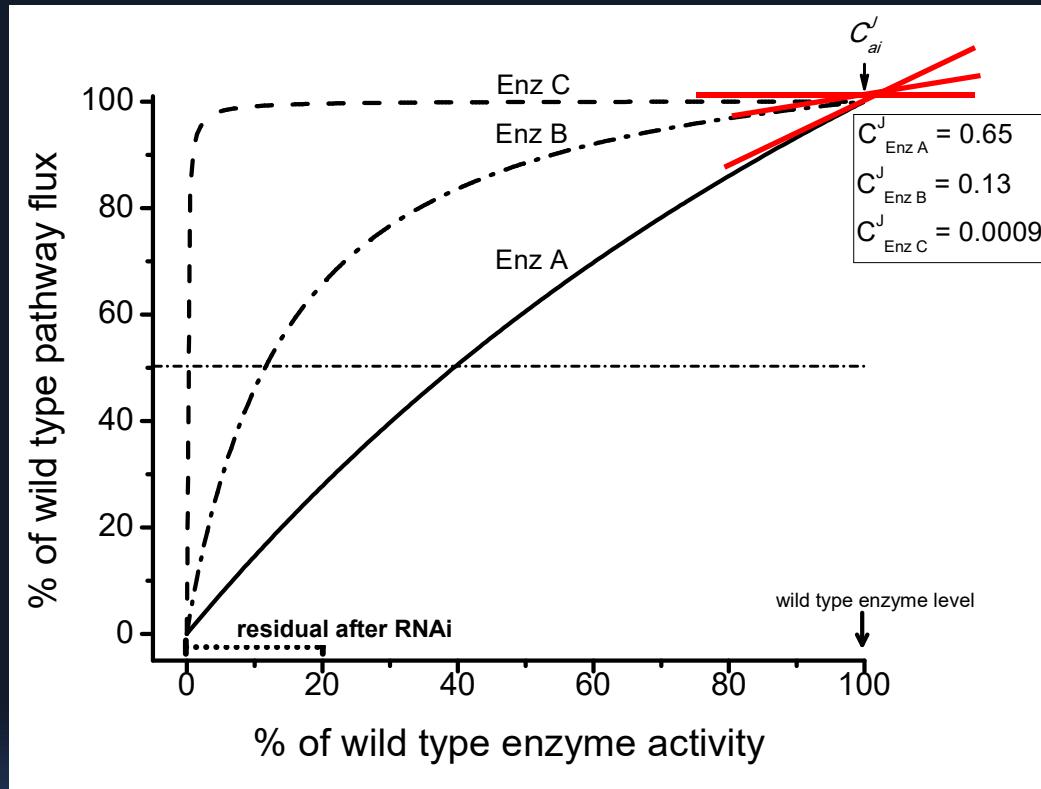
**In metabolic pathways there is not a unique rate-limiting step or bottleneck reaction**

# Metabolic Control Analysis (MCA) \*

\*Saavedra et al 2019 Curr Med Chem doi: 10.2174/0929867325666180917104242

MCA allows to quantitatively determine the degree of control that each enzyme has on the pathway flux (**flux control coefficient;  $C^J_{ai}$** )

- As the  $C^J_{ai}$  approaches to 1, means the enzyme has the highest control on flux
- The sum of all  $C^J_{ai}$  have to add up 1
- Usually there are two-three main controlling steps



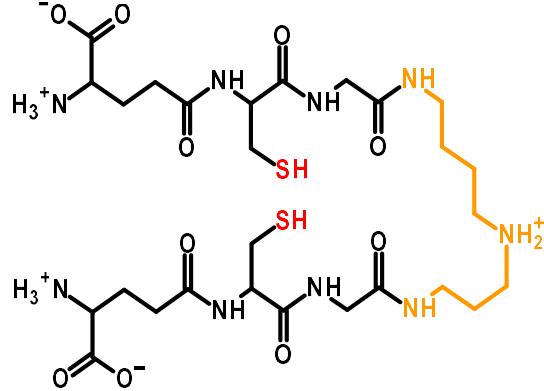
*The enzymes with the highest therapeutic potential are those with the highest  $C^J_{ai}$*

# Kinetic modeling and MCA to understand the controlling mechanisms in metabolic pathways

(and drug target prioritization for therapeutic intervention against parasites)

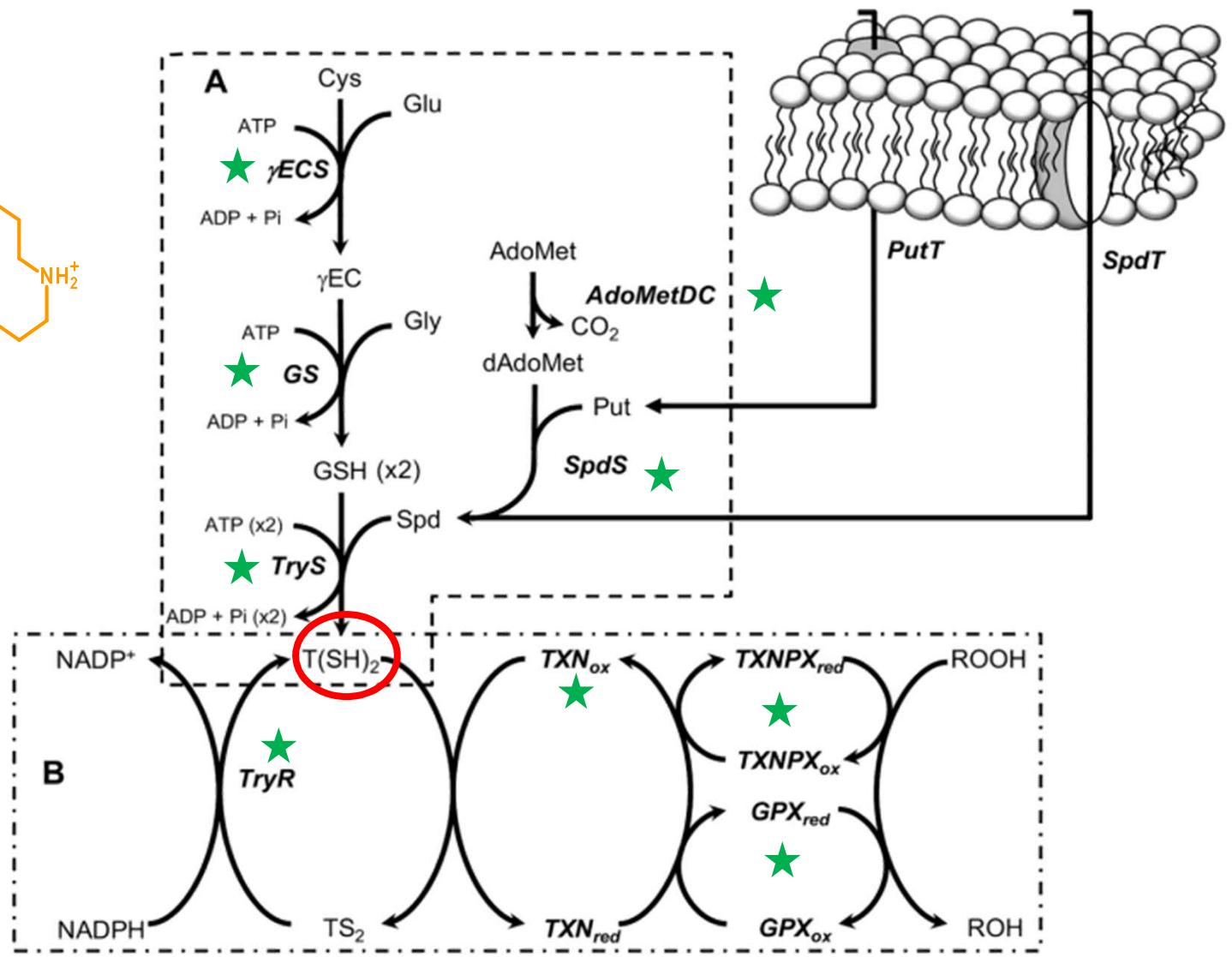
- Trypanothione metabolism in *Trypanosoma cruzi*
- Glycolysis in *Entamoeba histolytica*

# Tripanothione T(SH)<sub>2</sub>



González-  
Chávez et al.  
Redox Biology  
26 (2019)  
101231

## T(SH)<sub>2</sub>-dependent antioxidant metabolism in *Trypanosoma cruzi*



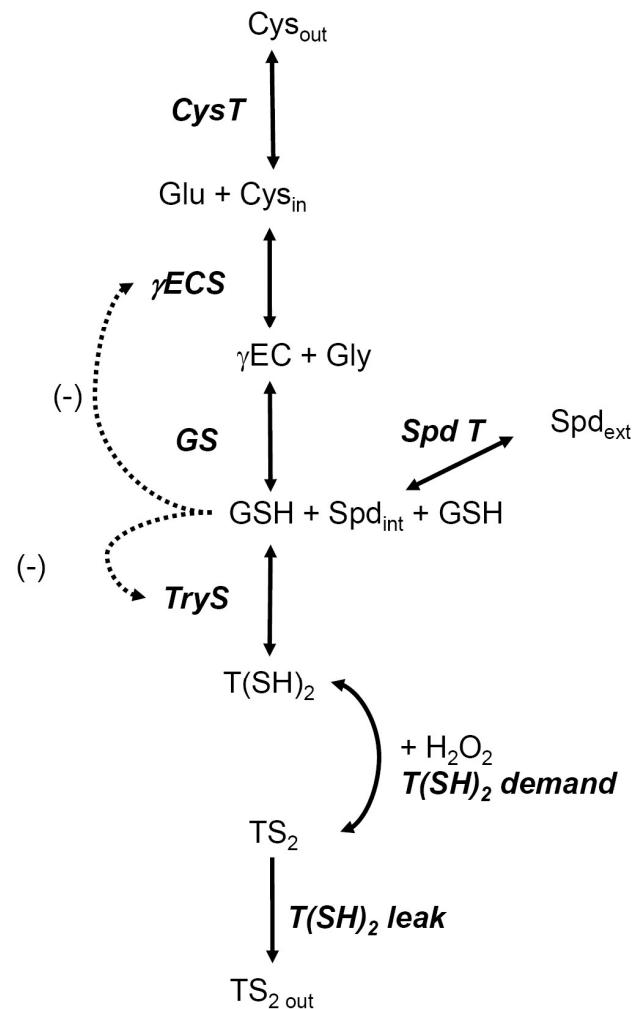
 All essential as determined by knockdown or knockout, thus all proposed as putative drug targets

## **Additional criteria for drug target prioritization**

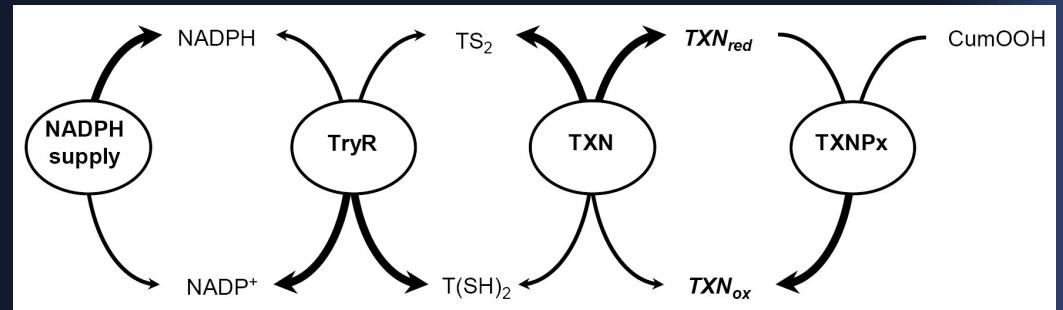
**-identification of the main controlling steps by kinetic metabolic modeling and MCA**

# Reactions included in the kinetic models

## Trypanothione synthesis

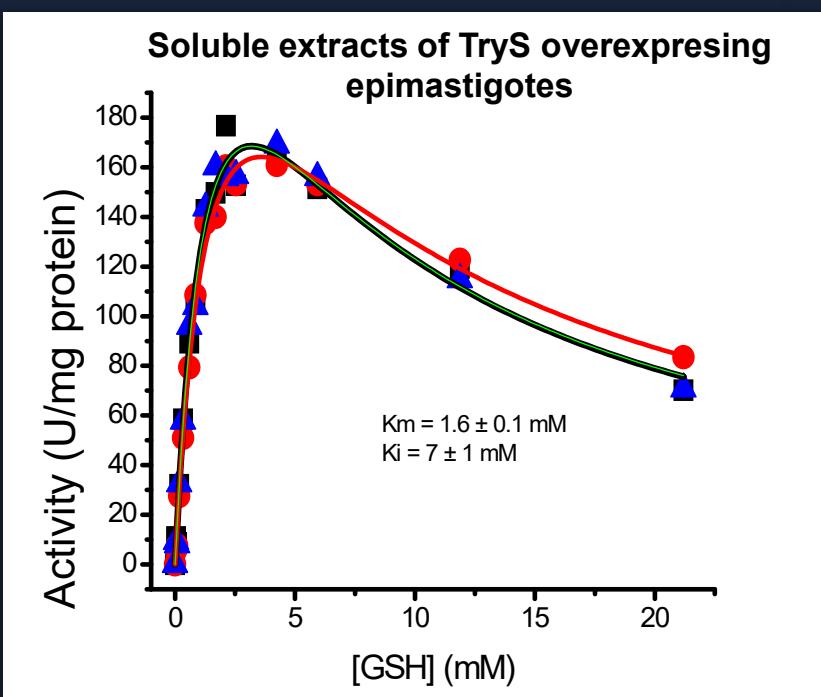
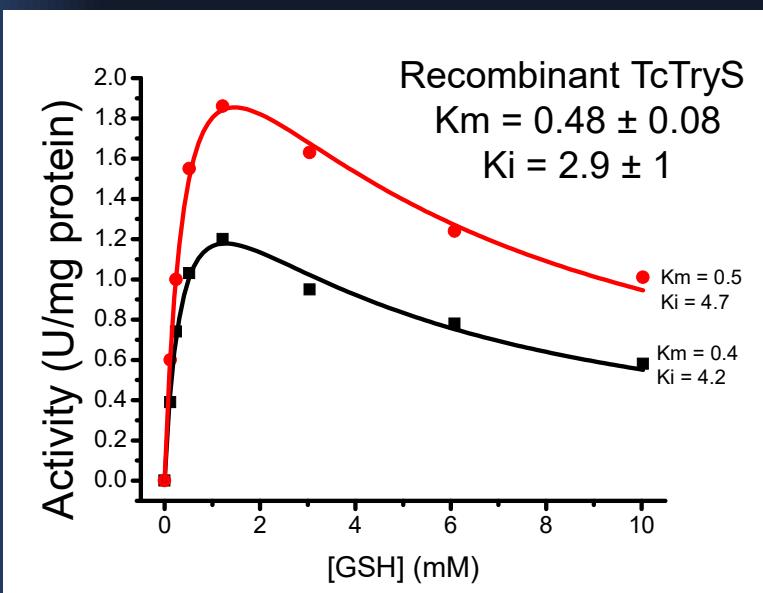


## Trypanothione-dependent peroxide reduction pathway



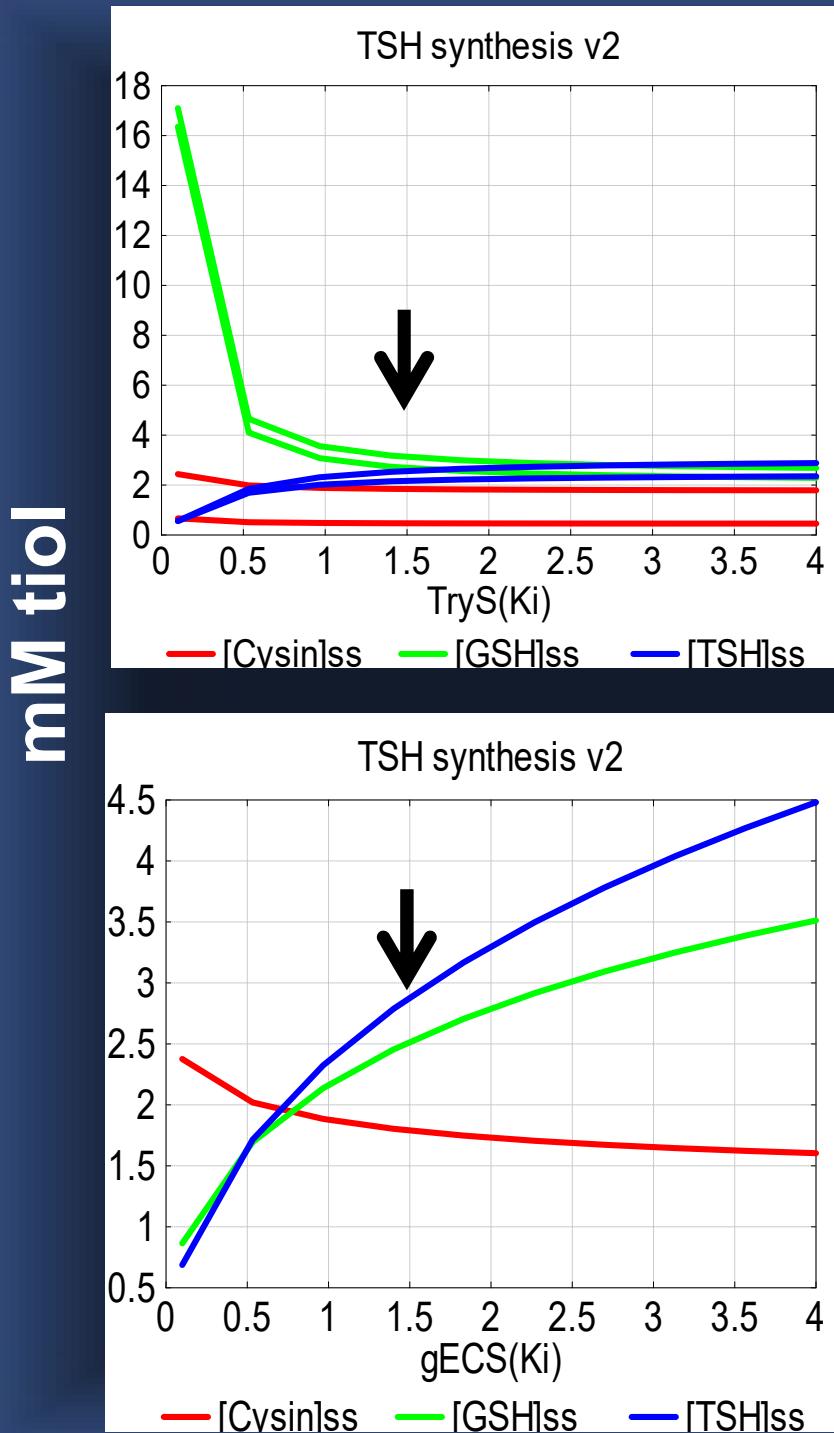
**Kinetic mechanisms**  
**Random bi-bi**  
**Random tri-uni**  
**Ordered-bi**  
**Ping pong**  
**Haldane**  
**Mass action**

# Regulatory loop: TryS inhibition by GSH



*Random Tri uni with mixed inhibiton by GSH*

$$\frac{\frac{V_m}{\alpha \cdot K_a \cdot K_b \cdot K_c \cdot \left(1 + \frac{I}{K_i}\right)} \cdot \left(A \cdot B \cdot C - \frac{P}{K_{eq}}\right)}{1 + \frac{A}{K_a} + \frac{B}{K_b} + \frac{C}{K_c} + \frac{A \cdot B}{\alpha \cdot K_a \cdot K_b} + \frac{A \cdot C}{\alpha \cdot K_a \cdot K_c} + \frac{B \cdot C}{\alpha \cdot K_b \cdot K_c} + \frac{A \cdot B \cdot C}{\alpha \cdot K_a \cdot K_b \cdot K_c} + \frac{A \cdot I}{\alpha \cdot K_a \cdot K_i} + \frac{B \cdot I}{\alpha \cdot K_b \cdot K_i} + \frac{C \cdot I}{\alpha \cdot K_c \cdot K_i} + \frac{P}{K_p}}$$



## Concentration control coefficients

TryS inhibition by GSH has local homeostatic effects on GSH

	$C_{[GSH]}_{ai}$	$C_{[TSH2]}_{ai}$
CysT	0.09	0.11
gECS	0.74	0.91
TryS	-0.74	0.18
TSH demand	-0.01	-0.22
TSH leak	-0.06	-0.98

$\gamma$ ECS inhibition by GSH has higher homeostatic effects on  $T(SH)_2$  than on GSH concentrations

# Kinetic models simulations

## T(SH)<sub>2</sub> synthesis

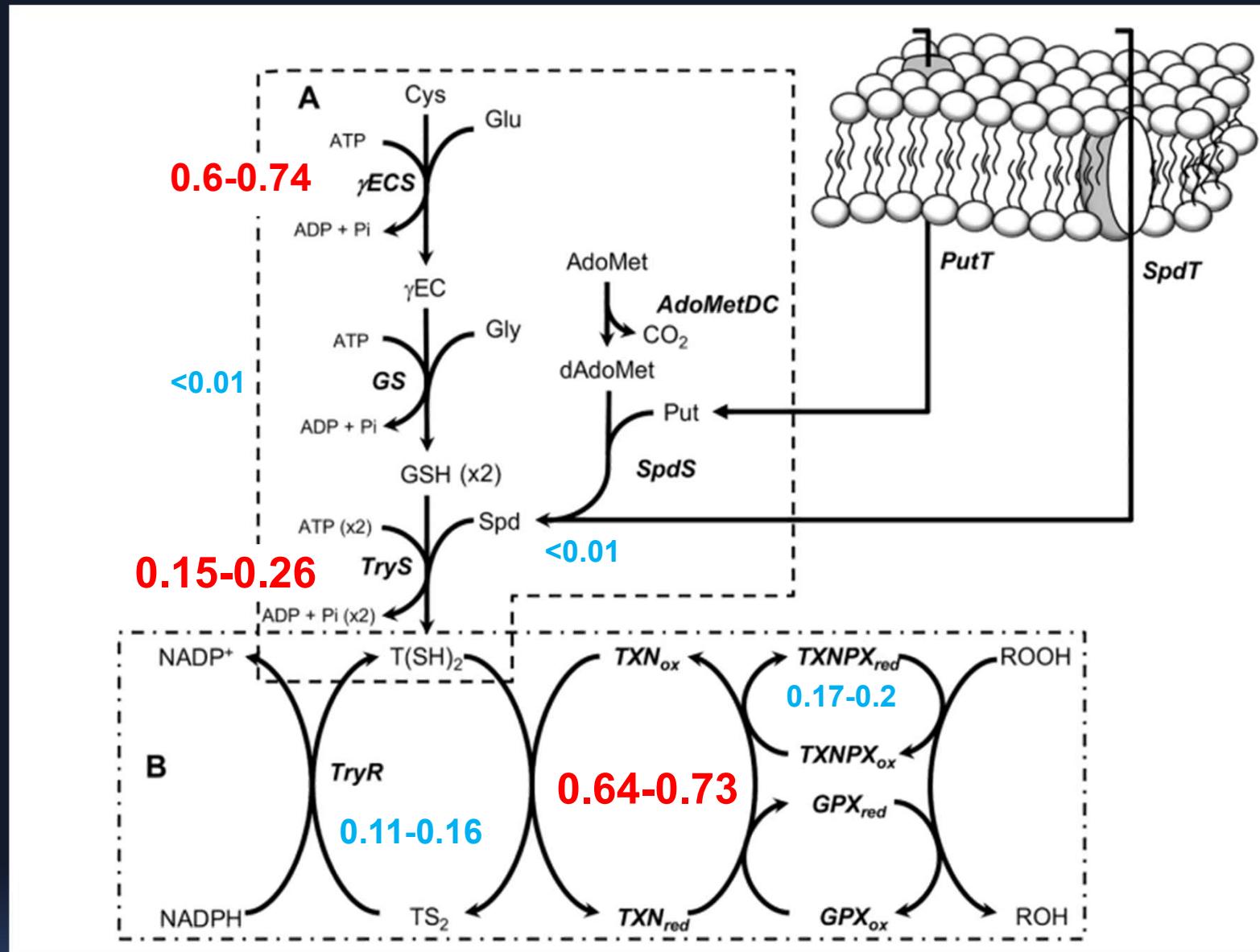
[Metabolite] (mM)	<i>In vivo</i>	Model
Cysin	1 ± 0.2	0.5
GSH	1.4±0.4	1.36
Spd	0.8±0.2	1.06
T(SH) <sub>2</sub>	0.9±0.4	0.75
pathway flux (nmol/min*mg cell protein)	0.6±0.2 (max)	0.12

## Peroxide reduction

[Metabolite] (mM)	Ex vivo	Model
T(SH) <sub>2</sub>	0.45±0.4	0.465
TXN ox	0.022-0.078	0.083- 0.089
Pathway flux (nmol/min*mg cell protein)	11±5 (max)	6.1-7.8

- ❖ The models can simulate the pathways behaviors

# Flux control coefficients ( $C_{ai}^J$ ) of the antioxidant system in *T. cruzi* obtained by kinetic modeling



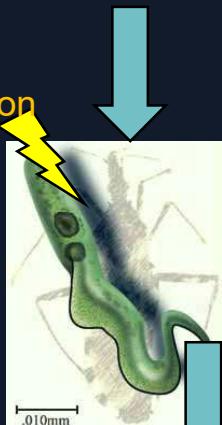
# In vivo determination of the flux control coefficients in *T. cruzi* trypanothione metabolism

## Experimental procedure

### Gene constructions

1. pTREXn
2. γECS
3. TryS
4. TryR
5. TXN

### Transfection



### Cloning



WT  
Mock  
Overexpressing

Enzymatic activities

Oxidative stress handling

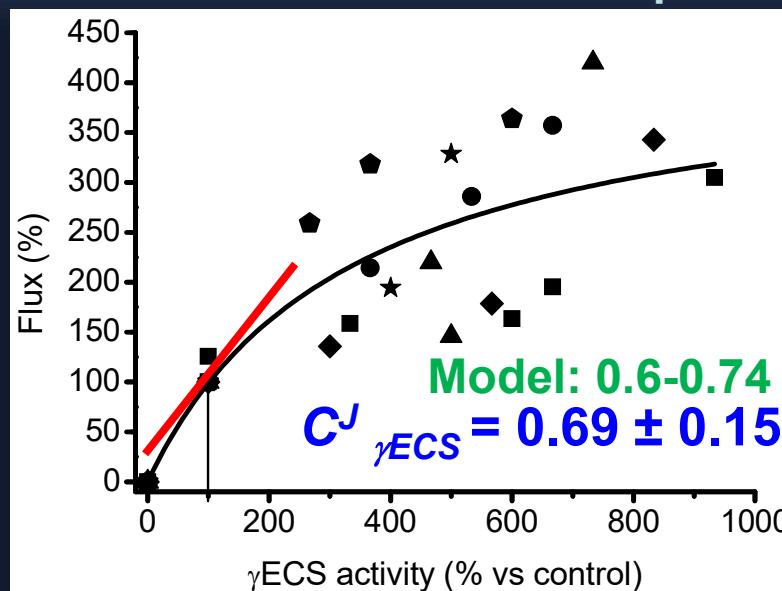
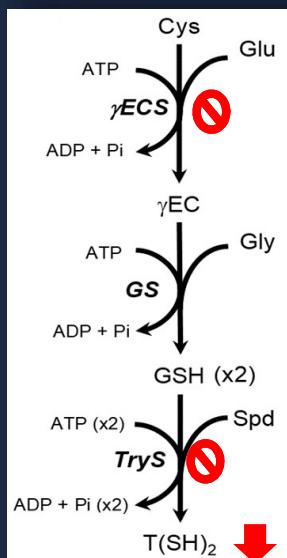
Metabolic fluxes

Metabolite concentrations

Peroxide resistance

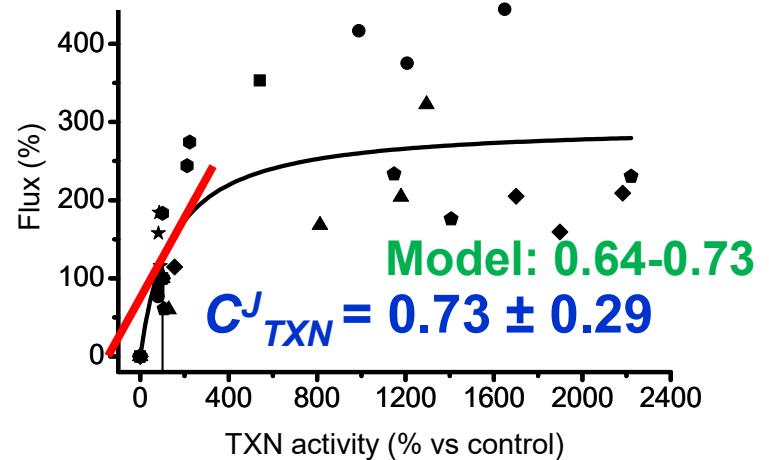
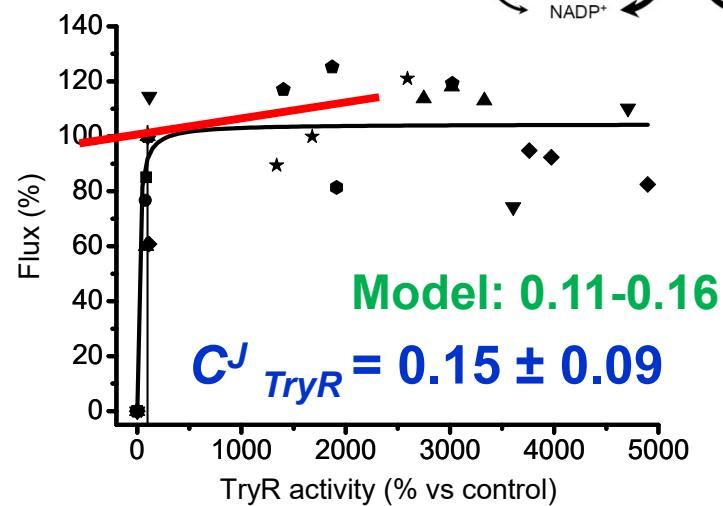
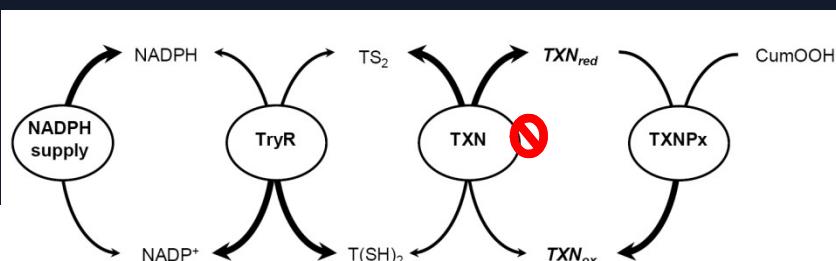
Flux control coefficient

# *In vivo* flux control coefficients are similar to those predicted by kinetic modeling



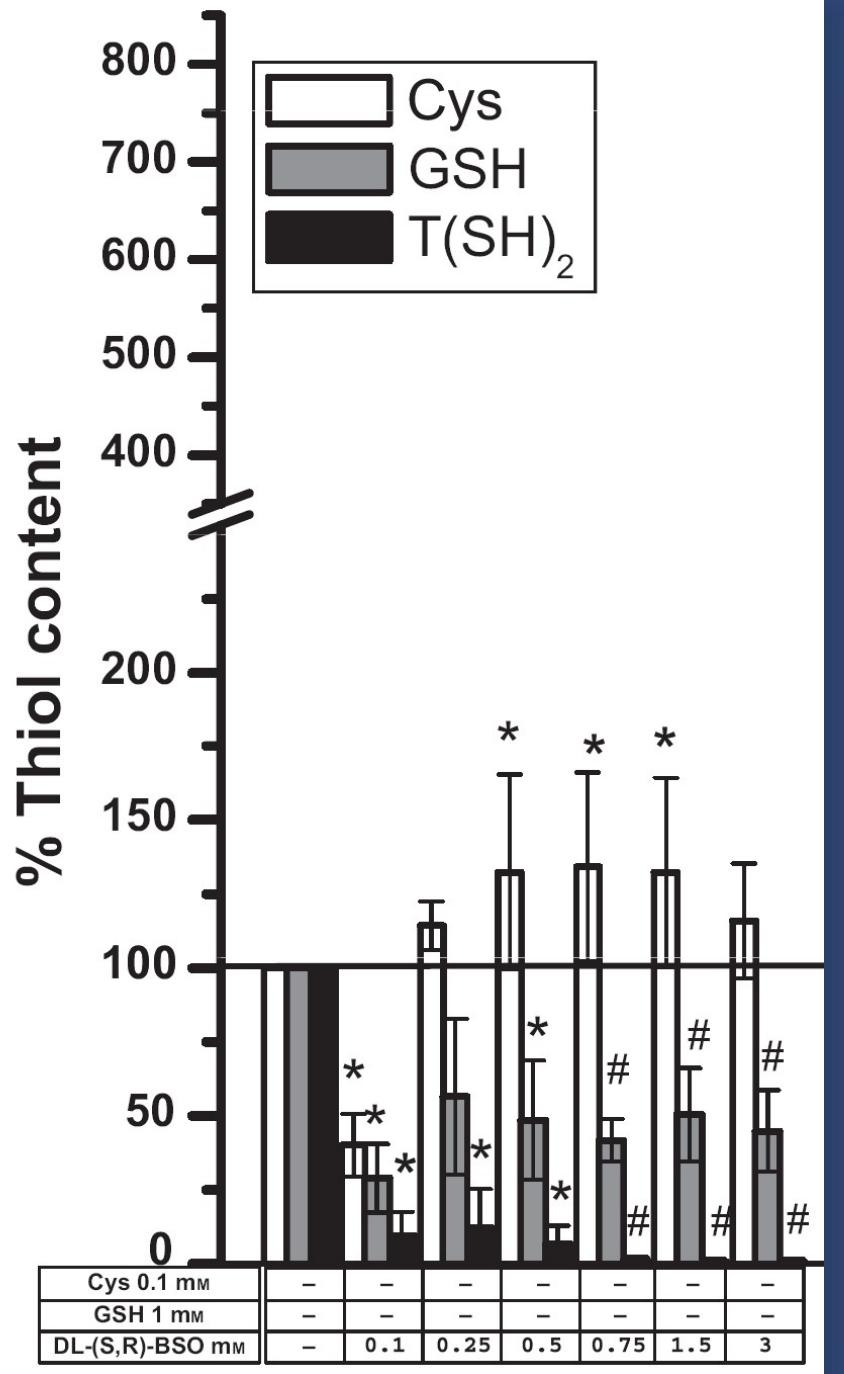
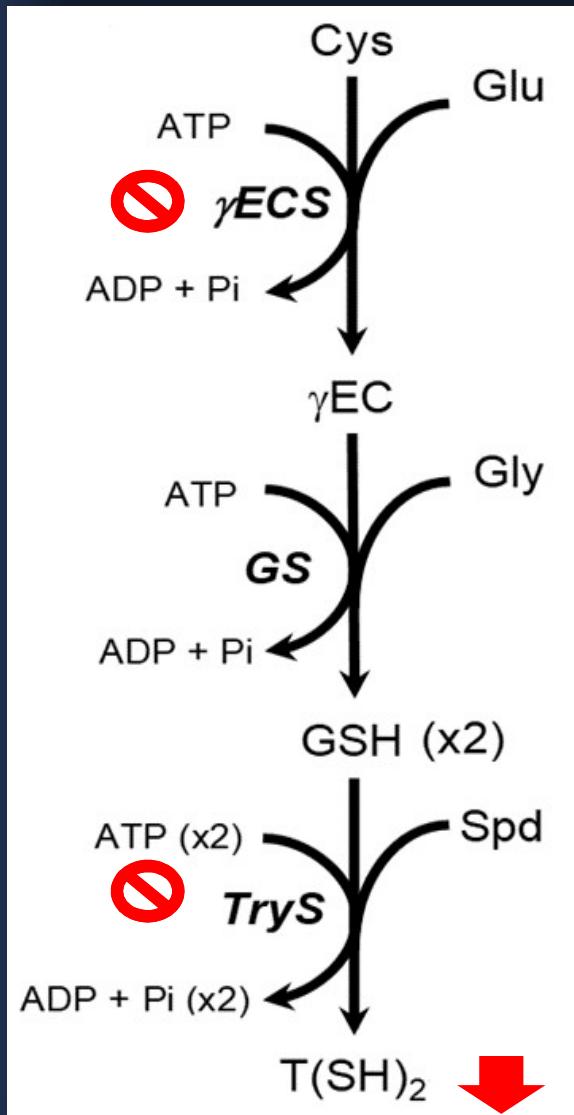
González-Chávez et al.  
Redox Biology (2019) 101231

$$C^J_{\text{TryS}} = 0.15-0.26$$



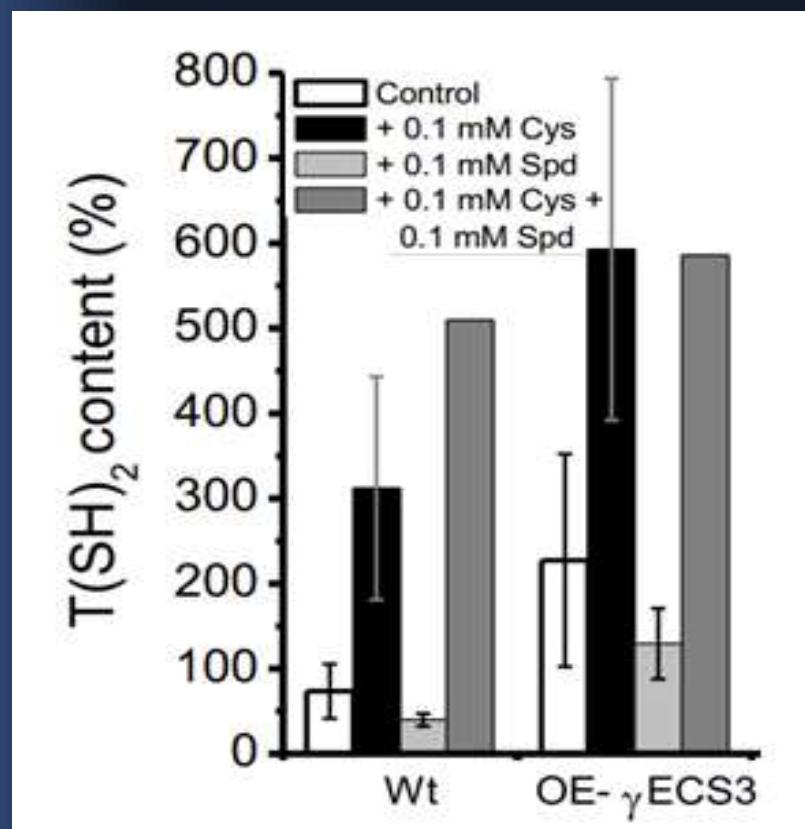
$\gamma$ ECS, TRYS AND TXN INHIBITION  
WILL AFFECT THE ANTIOXIDANT  
DEFENSE IN *T. CRUZI*

# Parasites treated with BSO decreases T(SH)<sub>2</sub> because it inhibits $\gamma$ ECS and TryS inhibition

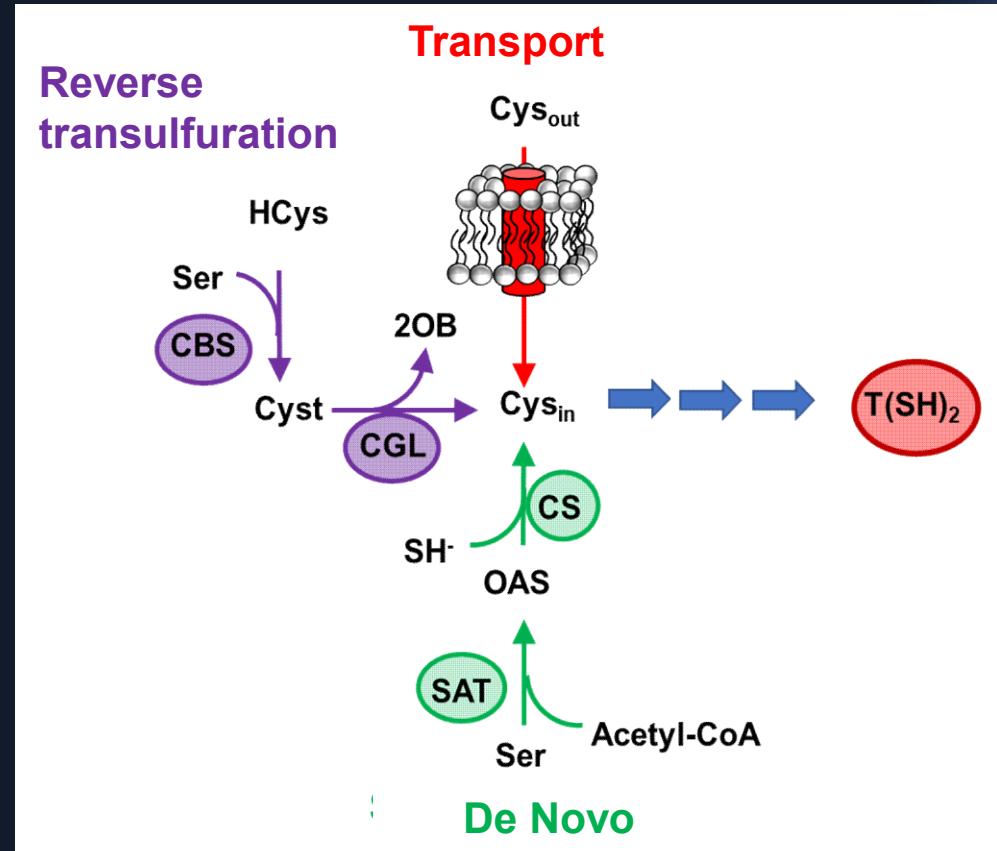


# According to the model, cysteine is limiting for $T(SH)_2$ biosynthesis

Epimastigotes supplied with cysteine (Cys) but not with spermidine (Spd), increased  $T(SH)_2$  content.

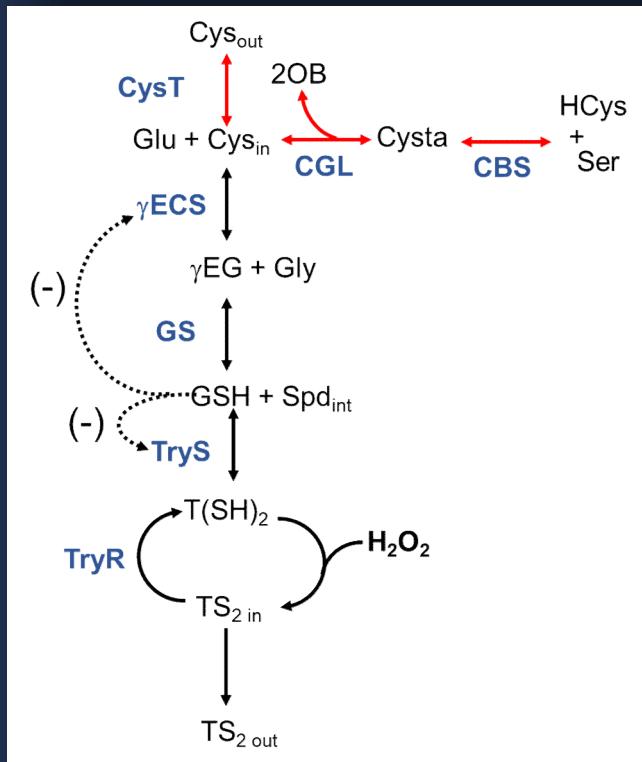


## Pathways of Cys supply in *T. cruzi*



# Kinetic model with the reverse transulfuration pathway of Cys synthesis

## Ping pong kinetics



Intermediary (mM)	In vivo	Model
Cys in	1 ± 0.2	2.1
GSH	1.4 ± 0.4	1.8
TSH2	0.9 ± 0.4	1.36
Cysta	0.88 ± 0.5	2.2
Flux T(SH) <sub>2</sub> synthesis	0. 6 ± 0.2 max	0.18
Flux Cys synthesis	1.13 ± 0.3 max	0.4

Flux in nmoles /min\*mg cell protein

## **$C^J_{ai}$ on T(SH)<sub>2</sub> synthesis**

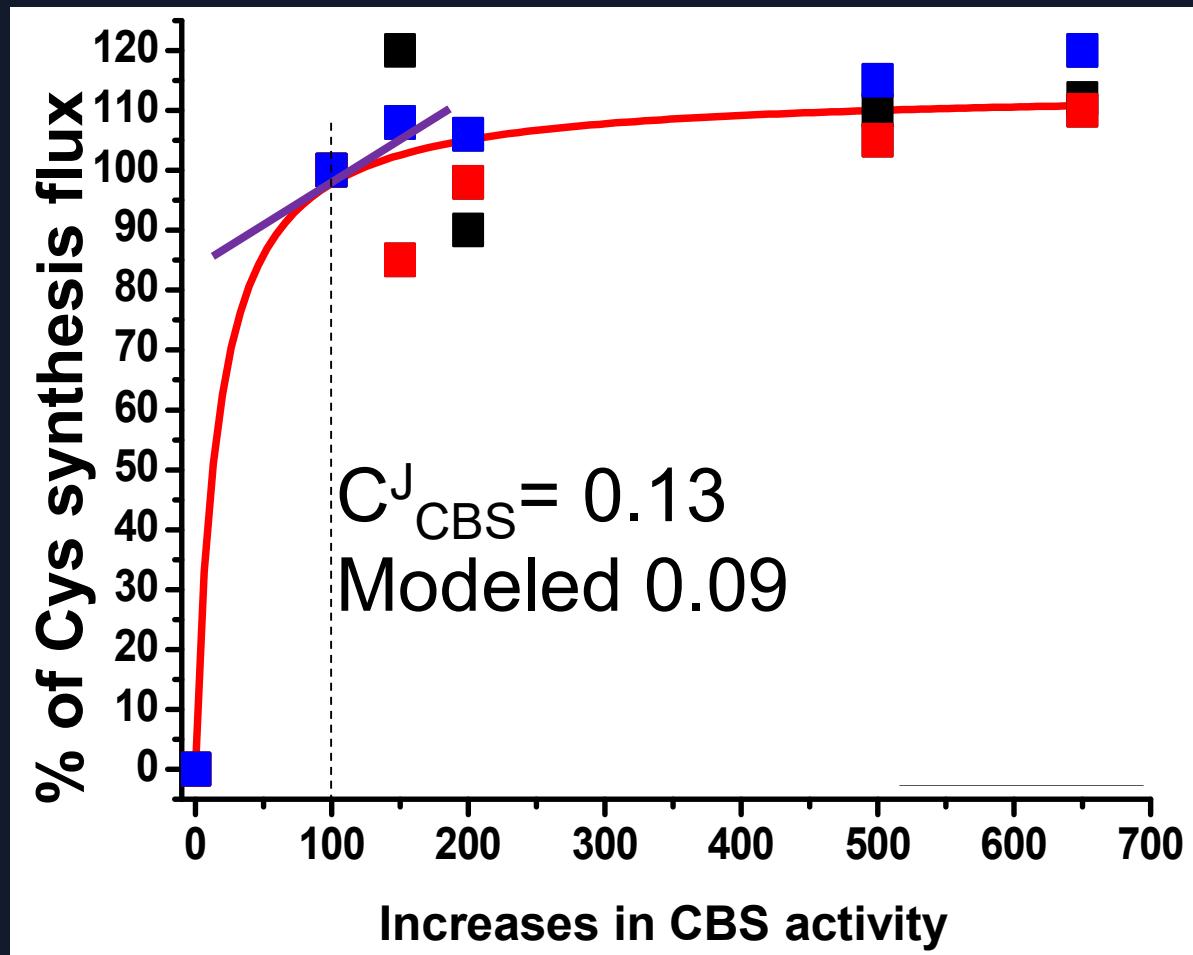
$C^J CBS + CGL$	0.05
$C^J \gamma ECS$	0.7
$C^J TryS$	0.21

## **$C^J_{ai}$ on Cys synthesis**

$C^J CBS$	0.09
$C^J CGL$	0.36
$C^J \gamma ECS$	0.34
$C^J TryS$	0.1

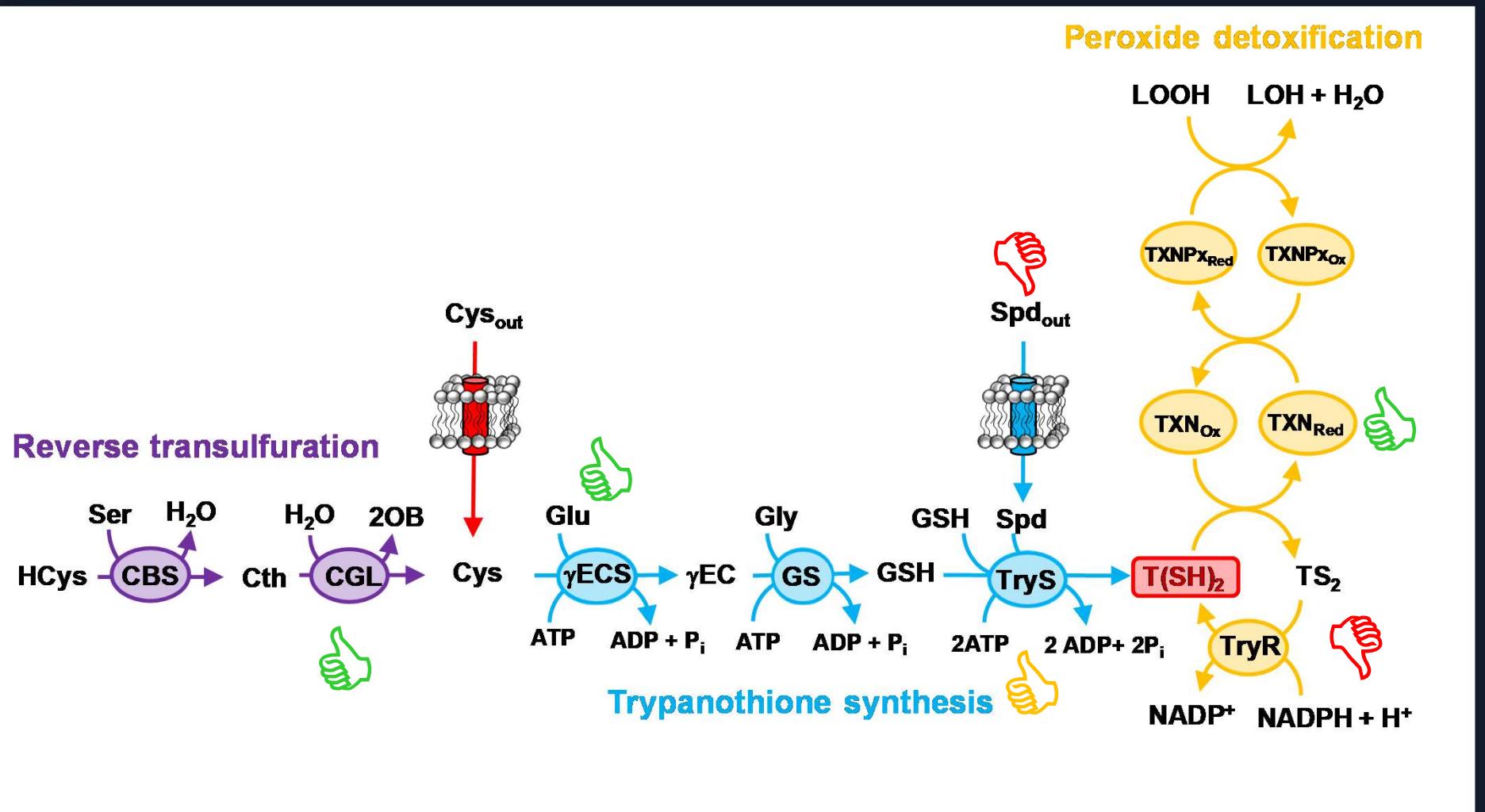
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## Cystathione $\beta$ synthase flux control coefficient on Cys synthesis



**CGL has high control on Cys synthesis flux**

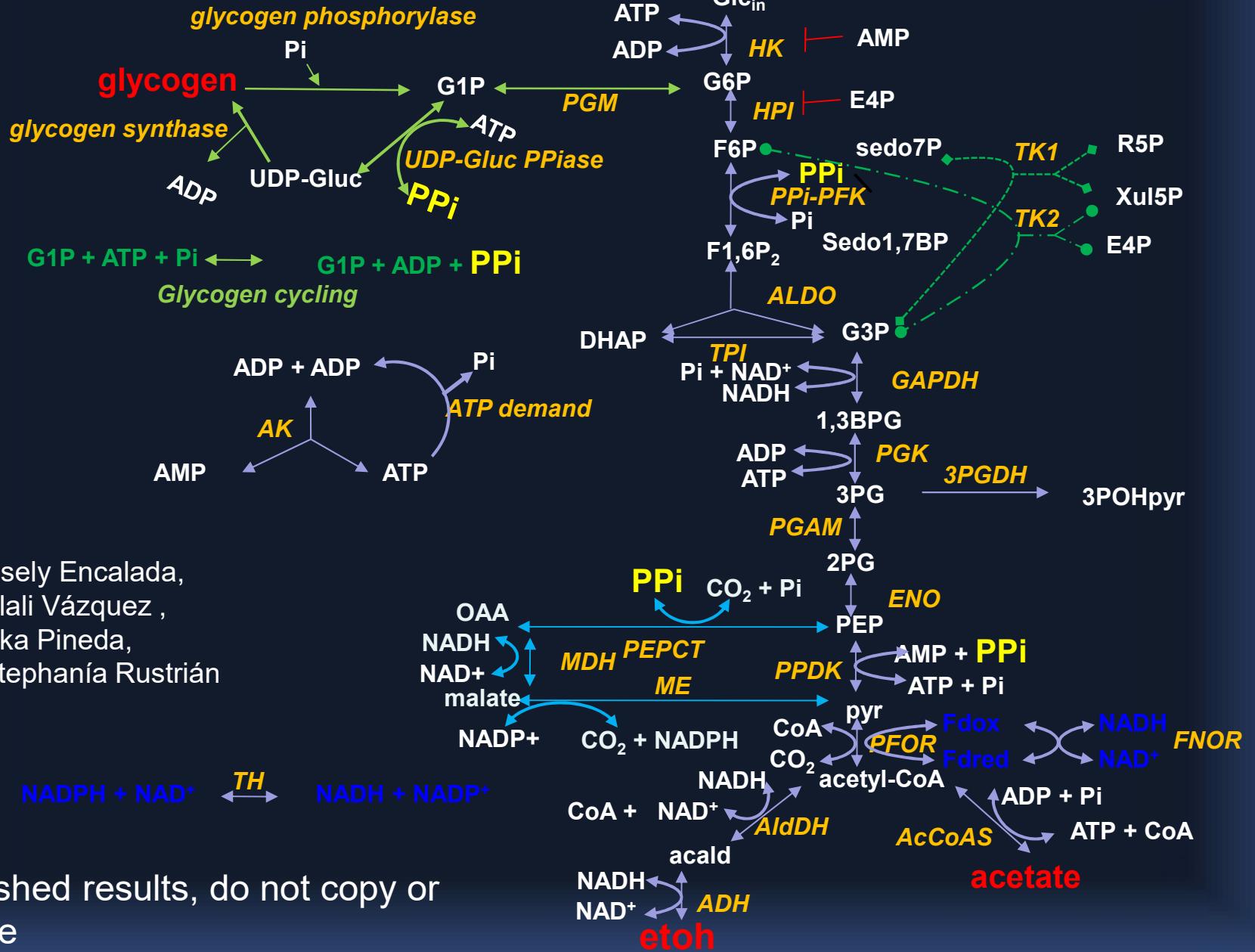
# Enzymes with the highest therapeutic potential



**Kinetic modeling of *Entamoeba histolytica* glycolysis to understand its controlling mechanisms and identify putative drug targets**

# PPi-dependent glycolysis of *Entamoeba histolytica*

## Kinetic model reactions



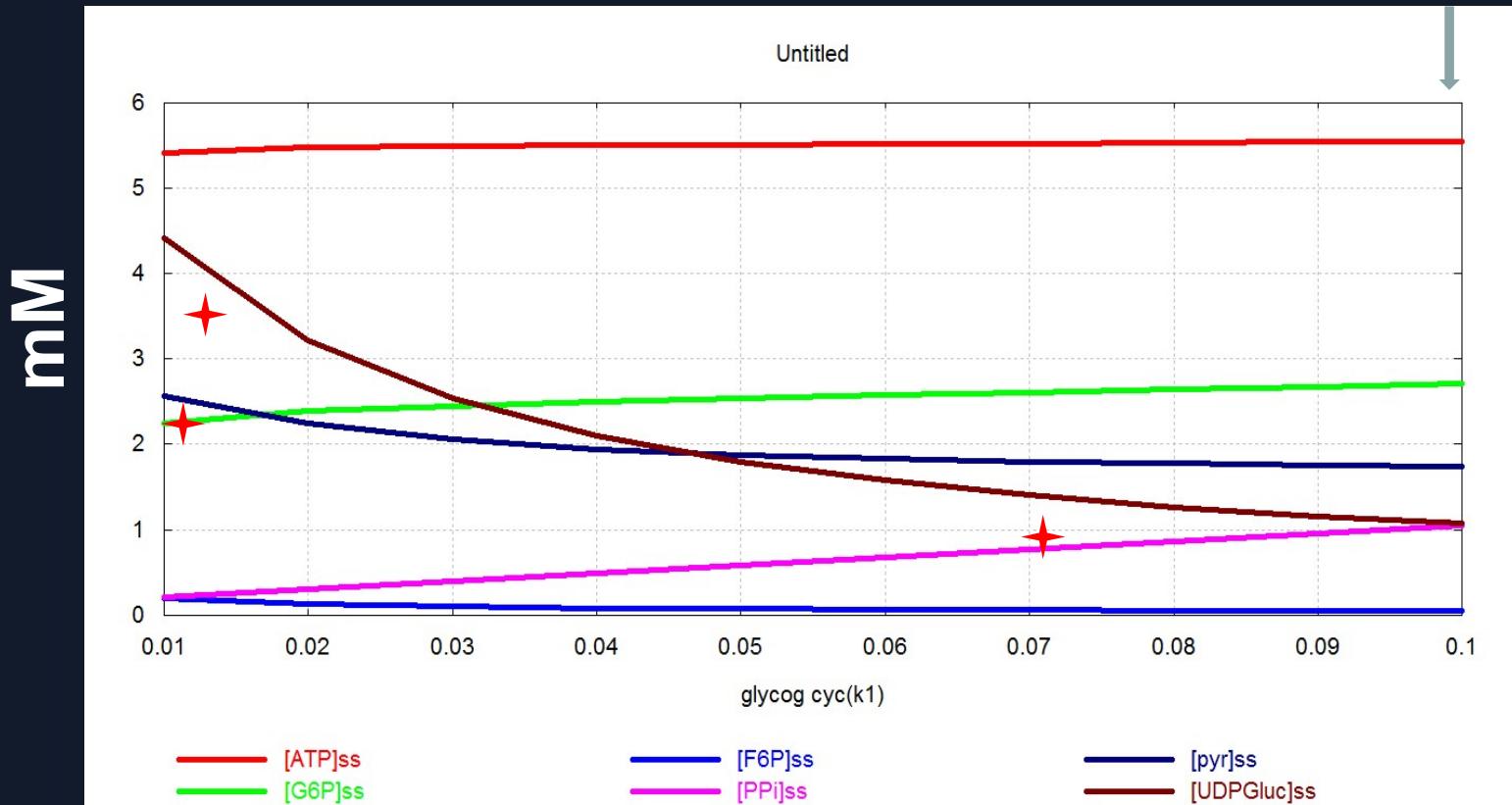
Rusely Encalada,  
Citlali Vázquez ,  
Erika Pineda,  
Estefanía Rustrián

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# Glycogen cycling (variation in k1)



Conserved moiety ATP + ADP + AMP + UDPGlc



Kinetic modeling suggests that glycogen cycling might be the most important source of PPi

Enzyme/process	model	Titration with inhibitors in live cells*	Elasticity analysis in live cells **
HXT	0.34		
HK	0.02		
Glycogen degradation	0.39		
HPI	0.01		
PGM	0.002		
UDPGlucPPiase Glycog synthase	-0.06 -0.03		-0.13 -> -0.22
PPi-PFK	0.014		
ALDO	0.015		
TPI	0.0005		
GAPDH	0.01		
PGK	0.006		
PGAM	0.28		
ENO	0.03		
PPDK	0.001		
PFOR	0.0003	0.07 (DPI)	0.13
AldDH + ADH	0.16 + 0.05	0.33 (disulfiram)	0.18
AcCoAS	-0.09	-0.05 knock-down	-0.08

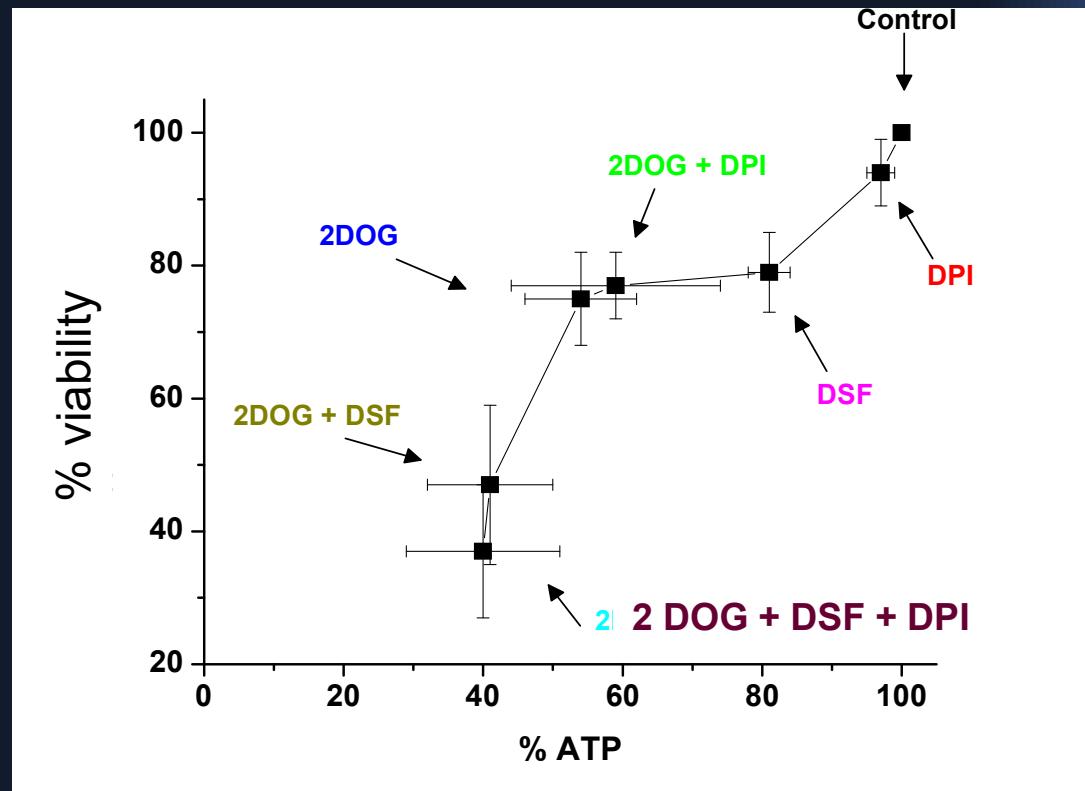
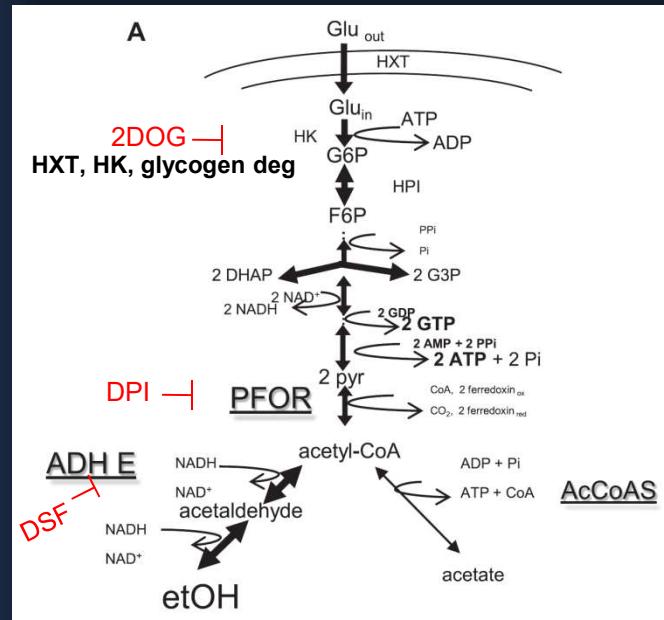
## Flux control coefficients ( $C^{J_{etoh}}_{vi}$ ) on EtOH flux determined through different MCA strategies

- Main controlling steps are: HXT, glycogen degradation, PGAM and ADHE
- The control of the pathway flux predicted by pathway modeling is similar to that determined in live cells.

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\*Pineda et al 2013 FEBS Lett  
\*\* Pineda et al 2015 FEBS J

# Effect of the Inhibition of the main controlling steps of amebal glycolysis on ATP content and cell viability



10 mM glucose, 30 mM DOG, 50 nM DSF, 100 nM DPI, 2h

Pineda et al 2015 FEBS J

**The most controlling enzymes can be proposed as relevant drug targets to decrease the glucose catabolism in amoebas.**

# **General conclusions**

- Kinetic modeling allows understanding of regulatory and controlling mechanisms of metabolic pathways
- Kinetic modeling and MCA helps to identify the main controlling steps which can be proposed as drug target candidates.

- Acknowledgments

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